Measuring Coherent Motions from Redshift Distortions

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Motivation

Decomposition of spectra in redshift space

Practice of decomposition using mocking maps

Optimizing redshift survey for cosmological purpose

Current measurement of coherent motions

Cosmological test of GR using WL and coherent motions

Conclusion

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Dark energy study prospects

Precision measurements of distance, growth, and curvature: it is desirable for future surveys to provide results of the distance and growth of structure, so that different theoretical models can be discernible.

Is dark energy a cosmological constant? : w=-1 even with generalized parameterization of all possibilities, e.g. variation of w, screening effect, induced anisotropy etc.

Is dark energy isotropic and homogeneous? : we need examine the distribution, mean, and rms value of w over all the pixels to see.

Is acceleration caused by modified gravity instead? : we need at least two different probes, WL and coherent motions.

Wide-deep surveys

Photometric wide-deep survey

Spectroscopic wide-deep survey



Beyond Standard Models

With the level of precision available in these surveys, what they tell us about fundamental physics? : whether we can test GR cosmologically, whether we can constrain beyond Standard Model of particle physics.

What can a wide deep survey tell us about the basic assumptions behind the standard cosmology? : test cosmological principle (isotropy and homogeneity), and Gaussianity.

What are the technical challenges to making these future surveys productive ?

Departures from standard DE



Observational service for theoretical models



Jain, Zhang 2008;YSS, Koyama 2009

Next generation of LSS test



Next generation of LSS test



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Developed techniques

Velocity measurements of nearby supernovae

Gordon, Land, Slosar (2008)

Velocity measurements of nearby galaxies

Feldman, Watkins, Hudson (2009) Watkins, Feldman, Hudson (2009) Lavaux, Tully, Mohayaee, Colombi (2010)

Analyzed CMB fluctuations on directions of X-ray clusteres

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Measuring coherent motions from redshift distortions

YSS, Pervical (2008) White, YSS, Pervical (2009) YSS, Sabiu, Nichol, Miller (2010) YSS, Sabiu, Kayo, Nichol (2010)

Developed techniques

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Correlation in redshift space

Galaxies (or Clusters) measure correlations amongst large scale local inhomogeneities, while the observed distortions in these correlations in redshift space can be used to extract information about peculiar velocities.

 $P_{s}(k,\mu) = P_{gg}(k) + 2\mu^{2}P_{g\Theta}(k) + \mu^{4}P_{\Theta\Theta}(k)$

Squeezing effect at large scales

(Kaiser 1987)

Finger of God effect at small sclaes (Jackson 1972)

Fisher analysis to decompose real spectra

We find that we can decompose peculiar velocity from the observed spectra in redshift space without using β . Errors can be estimated using Fisher matrix analysis, $P_s(k,\mu) = P_{gg}(k) + 2\mu^2 P_{g\Theta}(k) + \mu^4 P_{\Theta\Theta}(k)$

 $F_{\alpha\beta} = A \int k^2 dk \int d\mu \ dP_s(k,\mu) / dq_\alpha \ (V_{eff}/P_s)^2 \ dP_s(k,\mu) / dq_\beta$

where $q_{\alpha} = (P_{gg}, P_{g\Theta}, P_{\Theta\Theta})$.

But we are not able to know all spectra, as we observe only monopole and quadrupole precisely,

> $P_{s}(k,\mu) = P_{gg}(k) + 2\mu^{2}P_{g\Theta}(k) + \mu^{4}P_{\Theta\Theta}(k)$ = $(P_{gg} + 2/3P_{g\Theta} + 1/5P_{\Theta\Theta}) P_{0}(\mu)$ + $(4/3 P_{g\Theta} + 4/7P_{\Theta\Theta}) P_{2}(\mu)$ + $8/35P_{\Theta\Theta} P_{4}(\mu)$

Fisher analysis to decompose real spectra

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where $q_{\alpha} = (P_{gg}, P_{g\Theta}, P_{\Theta\Theta})$.

But we are not able to know all spectra, as we observe only monopole and quadrupole precisely,

 $P_{s}(k,\mu) = P_{gg}(k) + 2\mu^{2}P_{g\Theta}(k) + \mu^{4}P_{\Theta\Theta}(k)$

The assumed perfect cross-correlation between P_{gg} and $P_{\Theta\Theta}$, so we convert measured $P_{g\Theta}$ into $P_{\Theta\Theta}$ using $P_{g\Theta}/\sqrt{P_{gg}}P_{\Theta\Theta}$ =1.

Validation of perfect cross-correlation



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where $q_{\alpha} = (P_{gg}, P_{\Theta\Theta})$.

 $P_{s}(k,\mu) = P_{gg}(k) + 2\mu^{2} \sqrt{P_{gg}} P_{\Theta\Theta} + \mu^{4} P_{\Theta\Theta}(k)$

Estimated coherent motion spectra, $P_{\Theta\Theta}$



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$P_s(k)$ from time streaming Halo map

The Horizon simulation by Teyssier et.al.

Time streaming halo caltalogue

http://www.project-horizon.fr

Medium redshift z=0.8

Total volume 1Gpc³/h³



$P_{s}(k)$ from time streaming Halo map $P_{s}(k,\mu) = P_{gg}(k) + 2\mu^{2}\sqrt{P_{gg}(k)}P_{\Theta\Theta}(k) + \mu^{4}P_{\Theta\Theta}(k)$



YSS, Kayo 2010

$P_{s}(k,\mu)$ in polar coordinate $P_{s}(k,\mu) = P_{gg}(k) + 2\mu^{2}\sqrt{P_{gg}(k)P_{\Theta\Theta}(k)} + \mu^{4}P_{\Theta\Theta}(k)$



YSS, Kayo 2010

Decomposition in Kaiser limit

As $P_s(k,\mu)$ is given in polar coordinate, we can decompose $P_{\Theta\Theta}$ from measured spectra in each given bin μ using fitting formulation,

 $\chi_{i}^{2} = \Sigma_{p} \Sigma_{q} \left[P_{s}^{ob}(k_{i}, \mu_{p}) - P_{s}^{\dagger h}(k_{i}, \mu_{p}) \right] Cov^{-1}{}_{pq}(k_{i}) \left[P_{s}^{ob}(k_{i}, \mu_{q}) - P_{s}^{\dagger h}(k_{i}, \mu_{q}) \right]$

where $P_s^{\text{th}}(k_i, \mu_p) = P_{gg}(k_i) + 2\mu_p^2 \sqrt{P_{gg}(k_i)} P_{\Theta\Theta}(k_i) + \mu_p^4 P_{\Theta\Theta}(k_i)$.



Velocity dispersion effect



YSS, Kayo 2010

Decomposition in Kaiser limit

As $P_s(k,\mu)$ is given in polar coordinate, we can decompose $P_{\Theta\Theta}$ from measured spectra in each given bin μ using fitting formulation,

 $\chi_{i}^{2} = \sum_{p} \sum_{q} \left[P_{s}^{ob}(k_{i},\mu_{p}) - P_{s}^{th}(k_{i},\mu_{p}) \right] Cov^{-1}{}_{pq}(k_{i}) \left[P_{s}^{ob}(k_{i},\mu_{q}) - P_{s}^{th}(k_{i},\mu_{q}) \right]$

where $P_{s}^{th}(k_{1},\mu_{p}) = P_{gg}(k_{1}) + 2\mu_{p}^{2}/P_{gg}(k_{1})P_{cc}(k_{1}) + \mu_{p}^{4}P_{cc}(k_{1})$

 $P_{s}^{th}(k_{i},\mu) = [P_{gg}(k_{i}) + 2\mu_{p}^{2}P_{g\Theta}(k_{i}) + \mu_{p}^{4}P_{\Theta\Theta}(k_{i})] \exp[-(k_{i}\mu_{p}\sigma_{v})^{2}]$

Scoccimarro 2004

σ_v is estimated from P_{ΘΘ}(k_i) at all selected bins,
e.g. k_i=0.03, 0.05, 0.07, 0.09 h/Mpc

 $\chi^2 = \Sigma_i \Sigma_p \Sigma_q \left[P_s^{ob}(k_i, \mu_p) - P_s^{th}(k_i, \mu_p) \right] Cov^{-1}{}_{pq}(k_i) \left[P_s^{ob}(k_i, \mu_q) - P_s^{th}(k_i, \mu_q) \right]$

YSS, Kayo 2010

Decomposed Peculiar velocity Fisher matrix (unfilled contours) Measurement (filled contours)



Cut-off strategy



YSS, Kayo 2010

Threshold limit



Detectability can be extended up to k ~ 0.1 h/Mpc at the cost of weakened constraint.

YSS, Kayo 2010

Measurements

Measurements from Wiggle-z experiments

Four tomographic bins at z=0.2, 0.4, 0.6, 0.8

Measurements



Blake, et.al. 2011

Model independent extraction

Tang, Kayo, Takada 2011 Snap shot at z=0 Total volume 1Gpc³/h³

 $P_{s}(k,\mu) = [P_{gg}(k) + 2\mu^{2} \sqrt{P_{gg}(k)} P_{\Theta\Theta}(k) + \mu^{4} P_{\Theta\Theta}(k)] \exp[-(k\mu_{p}\sigma_{v})^{2}]$

 $P_{s}(k,\mu) = [P_{gg}(k) + 2\mu^{2} \sqrt{P_{gg}(k)} P_{\Theta\Theta}(k) + \mu^{4} P_{\Theta\Theta}(k)] [1 - (k\mu_{p}\sigma)^{2} + (k\mu_{p}\tau)^{4}/2]$

Decomposed $P_{XY}(k)$ of dark matter

 $P_{s}(k,\mu) = [P_{gg}(k) + 2\mu^{2} \sqrt{P_{gg}(k)} P_{\Theta\Theta}(k) + \mu^{4} P_{\Theta\Theta}(k)] \exp[-(k\mu_{p}\sigma)^{2}]$ $P_{s}(k,\mu) = [P_{gg}(k) + 2\mu^{2} \sqrt{P_{gg}(k)} P_{\Theta\Theta}(k) + \mu^{4} P_{\Theta\Theta}(k)] [1 - (k\mu_{p}\sigma)^{2} + (k\mu_{p}\tau)^{4}/2]$



Tang, Kayo, Takada 2011

Decomposed P_{XY}(k) of halo

$$\begin{split} \mathsf{P}_{s}(k,\mu) &= \left[\mathsf{P}_{gg}(k) + 2\mu^{2} \sqrt{\mathsf{P}_{gg}(k)} \mathsf{P}_{\Theta\Theta}(k) + \mu^{4} \mathsf{P}_{\Theta\Theta}(k)\right] \exp[-(k\mu_{p}\sigma)^{2}] \\ \mathsf{P}_{s}(k,\mu) &= \left[\mathsf{P}_{gg}(k) + 2\mu^{2} \sqrt{\mathsf{P}_{gg}(k)} \mathsf{P}_{\Theta\Theta}(k) + \mu^{4} \mathsf{P}_{\Theta\Theta}(k)\right] \left[1 - (k\mu_{p}\sigma)^{2} + (k\mu_{p}\tau)^{4}/2\right] \end{split}$$



Tang, Kayo, Takada 2011

P_s(k) from larger Halo map

The Horizon simulation at KIAS by Kim, Park, Gott Snap shot at z=0 Total volume 6.5³Gpc³/h³

Theoretical prior on FoG at linear regime

Two different approaches to formulate redshift distortion effect, 1) streaming model, 2) Kaiser effect,

1) streaming model: formulating FoG effect at smaller scale

2) Kaiser effect: formulating redshift distortion at large scale

The limit of streaming model at linear regime was derived in Fisher 1995, and shows the agreement between both approaches.

It is interesting to derive FoG effect on redshift distortion at linear regime using streaming model. We make the following assumption,

coherent v_z in Mpc/h unit << correlation length

Then,

 $P_{s}^{th}(k_{i},\mu) = [P_{gg}(k_{i}) + 2\mu_{p}^{2}P_{g\Theta}(k_{i}) + \mu_{p}^{4}P_{\Theta\Theta}(k_{i})] \exp[-(k_{i}\mu_{p}\sigma_{v})^{2}]$

Desjacques, Sheth 2009; YSS, et.al. 2011 Prepared

$P_{s}(k,\mu) = [P_{gg}(k) + 2\mu^{2}\sqrt{P_{gg}(k)}P_{\Theta\Theta}(k) + \mu^{4}P_{\Theta\Theta}(k)] \exp[-(k\mu_{p}\sigma_{v})^{2}]$



$Decomposed P_{\Theta\Theta}(k)$ $P_{s}(k,\mu) = [P_{gg}(k) + 2\mu^{2}\sqrt{P_{gg}(k)P_{\Theta\Theta}(k)} + \mu^{4}P_{\Theta\Theta}(k)] \exp[-(k\mu_{p}\sigma_{v})^{2}]$



Estimated coherent motion spectra, $P_{\Theta\Theta}$



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Cosmological constraint from decomposed $P_{\Theta\Theta}$

Spectra $P_{\Theta\Theta}$ are given by,

$$P_{\Theta\Theta}(k,a) = \frac{8\pi^2}{25} \frac{k}{H_*^4 \Omega_m^2} A_S^2 \left(\frac{kh}{k_p}\right)^{n_S - 1} T_{\Phi}^2(kh) g_{\Theta}^2(a).$$

CMB priors for cosmological test with $P_{\Theta\Theta}$, Primordial information – amplitude and spectral index Shape of spectra – transfer function We probe dark energy or modified GR using growth factor g_{Θ} , $d\delta_m/dt + \theta_m/a = 0$ $d\theta_m/dt + H\theta_m = k^2\Psi/a$

 $k^{2}\Phi = 3/2 H_{0}^{2}\Omega_{m} \delta_{m}/a + k^{2}\phi \qquad \Phi = -\Psi + \phi$ $(1+3\omega_{BD}) k^{2}\phi = -3H_{0}^{2}\Omega_{m} \delta_{m}/a - M^{2}\phi$

Dark energy constraint from $P_{\Theta\Theta}$



YSS 2011

Cosmological constraint from $P_{\Theta\Theta}$

Cosmological constraints from $P_{\Theta\Theta}$ are estimated using Fisher matrix analysis,

$$F_{mn}^{\Theta\Theta} = \sum_{k=1}^{N_k^{\text{cut}}} \sum_{z_j=0}^2 \frac{\partial P_{\Theta\Theta}(k_i, z_j)}{\partial x_m} \frac{1}{\sigma_{P_{\Theta\Theta}^{\text{dec}}}(k_i, z_j)^2} \frac{\partial P_{\Theta\Theta}(k_i, z_j)}{\partial x_n} \,.$$

Dark energy constraint from $P_{\Theta\Theta}$



YSS 2011

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Correlations in configuration space



Guzzo et.al. VIPER collaboration

Decomposition in configuration space

In the linear regime of the standard gravitational instability theory, the Kaiser effect (the observed squeezing due to coherent infall around large-scale strutures) can be written in the configuration space as,

$$\begin{split} \xi(\sigma,\pi) &= (g_{b}{}^{2}+g_{b}g_{\Theta}+g_{\Theta}{}^{2}) \xi_{0}(r) & \text{Monopole} \\ &- (g_{b}g_{\Theta}+g_{\Theta}{}^{2}) \xi_{2}(r) & \text{Quadrupole} \\ &+ g_{\Theta}{}^{2} \xi_{4}(r) & \text{Hexadecapol} \end{split}$$

The inverse signature in quadrupole induces squeezing effect. The leading order of monopole is galaxy-galaxy correlation, and the leading order of quadrupole is galaxy-velocity cross-correlation. Here we assume the perfect cross-correlation coefficient.

YSS, Sabiu, Nichol, Miller 2011

Variation of gb



 $\xi(\sigma,\pi) = (g_b^2 + g_b g_\Theta + g_\Theta^2) \xi_0(r)$

- $(g_b g_\Theta + g_\Theta^2) \xi_2(r)$

+ g_Θ² ξ₄(r)

YSS, Sabiu, Nichol, Miller 2011

Variation of g_{Θ}



 $\xi(\sigma,\pi) = (g_b^2 + g_b g_\Theta + g_\Theta^2) \xi_0(r)$

- $(g_b g_\Theta + g_\Theta^2) \xi_2(r)$

+ g_Θ² ξ₄(r)

YSS, Sabiu, Nichol, Miller 2011

Parameterizing $\xi(\sigma, \pi)$

 $\xi(\sigma,\pi) = (g_b^{*2} + g_b^{*} g_{\Theta}^{*} + g_{\Theta}^{*2}) \xi_0^{*}(r) - (g_b^{*} g_{\Theta}^{*} + g_{\Theta}^{*2}) \xi_2^{*}(r) + g_{\Theta}^{*2} \xi_4^{*}(r)$

In Kaiser effect:

 $\xi_{l}^{*}(r) = \int k^{2} dk / 2\pi^{2} D_{m}^{*}(k) j_{l}(kr)$

 $D_{m}^{*}(k) = 4/9 \ k^{4}/H^{*4} \omega_{m}^{2} \ D_{\Phi}^{*}(k) \qquad (H^{*} = 1/2997 \ Mpc^{-1})$ $D_{\Phi}^{*}(k) = 2\pi^{2}/k^{3} \ 9/25 \ \Delta_{\zeta_{i}}^{2} \ T_{\Phi}^{2}(k) \qquad (\Delta^{*}_{\zeta_{i}}^{2} = 2.43 \times 10^{-9} (k/k_{p})^{(ns-1)})$

In Kaiser effect + velocity dispersion:

 $\xi_{l}^{*}(r) = \int k^{2} dk d\mu / (2\pi)^{2} D_{m}^{*}(k) e^{-(k\mu\sigma v)^{2}} \cos(kr\mu) P_{l}(\mu)$

ξ(σ,π) diagram of SDSS DR7 LRG Kaiser effect (unfilled contours) Modified Kaiser effect (filled contours) Prediction with b=1.82 Measurement from SDSS DR7 LRG



Cut off for fitting

Cut off #1: perfect correlation is not available around k=0.1 h/Mpc Cut off #2: non-linear line of smearing effect



Measured bulk flow motions

Kaiser effect (unfilled contours) Modified Kaiser effect (filled contours)



Measured quantities from redshift distortions

z = 0.25 z = 0.38

$g_{\Theta}^* \equiv f\sigma_8^{M^*}$	0.39 ± 0.08 (0.41)	0.43 ± 0.08 (0.42)
σ _v (in h/Mpc)	3.1 ± 0.6 h/Mpc (3.2)	3.5 ± 0.6 h/Mpc (3.4)
σ _v ^{km} (in km/s)	277 ± 55 km/s (294)	300 ± 57 km/s (293)
β (Kaiser + v.d.)	0.32 ± 0.067	0.36 ± 0.075
β (Kaiser only)	0.30 ± 0.063	0.32 ± 0.065
b (Kaiser + v.d.)	1.82 ± 0.13	1.92 ± 0.16
b (Kaiser only)	1.96 ± 0.10	2.11 ± 0.10

Measured quantities from redshift distortions

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Measured coherent motions in discrepancy

Velocity measurements of nearby galaxies

Feldman, Watkins, Hudson (2009) Lavaux, Tully, Mohayaee, Colombi (2010)

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Kashlinsky, Atric-Barandela, Kocevski, Ebeling (2008) Kashlinsky, Atrio-Barandela, Kocevski, Ebeling (2009)

Measuring coherent motions from redshift distortions

YSS, Pervical (2008) White, YSS, Pervical (2009) Support LCDM USS, Seig, Schol, Miller (2010) YSS, Sabiu, Kayo, Nichol (2010)

Measured coherent motions in discrepancy

Bulk flow motions are averaged from directly measured peculiar velocity at local universe, which disagree with concordance LCDM model normalized with WMAP7.



Measured coherent motions in discrepancy

Velocity measurements of nearby galaxies

Possible presence Witkins Fedran Hudson (2009) Lavaux, Tully, Mohayaee, Colombi (2010) at near horizon scale

Analyzed CMB fluctuations on directions of X-ray clusteres Coherent motions against Kashlinsky, Atrio-Barandela, Kocevski, Ebeling (2008) CMB ashtirsky, Atrio-Barandela, Kocevski, Ebeling (2009)

Measuring coherent motions from redshift distortions Coherent motions YSS, Pervical (2008) White, YSS, Pervical (2009) in rest frame Sabiu, Nichol, Miller (2010) YSS, Sabiu, Kayo, Nichol (2010)

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Constraint on departure of $\Phi-\Psi$ using WL



Constraint on departure of $\Phi-\Psi$ using WL



Constraint on $\Phi-\Psi$ and Ψ using WL and CM



PV measures θ and estimates Ψ

Measured coherent motions from DR7



Constraint on departure of Ψ using CM



Constraint on $\Phi-\Psi$ and Ψ using WL and CM



PV measures θ and estimates Ψ

Constraint on $\Phi-\Psi$ and Ψ using WL and CM



Discussion

How to coherently combine both different statistics, BAO and coherent motions?

How to formulate theory of redshift distortion in model independent way? (open comments)

How to extend our study from dark matter limit to observable galaxies?

Other systematic uncertainties ?