

Effect of multi-field non-Gaussianities on the large-scale structure

Takahiro Nishimichi (IPMU)

**Atsushi Taruya (RESCEU)
Kazuya Koyama (ICG, Portsmouth)**

Outline

- brief review of **single-field** local-type nG on LSS
- effect of **multi-field** local-type nG on scale-dependent bias
 - bispectrum & trispectrum parametrized by (f_{nl}, g_{nl}, T_{nl})
 - more general cases with scale dependence

single-field local-type nG

Local-type NG and Large Scale Structure

local-type primordial Non-Gaussianity

$$\zeta(\mathbf{x}) = \zeta_G(\mathbf{x}) + \frac{3}{5} f_{nl} [\zeta_G^2(\mathbf{x}) - \langle \zeta_G^2 \rangle]$$

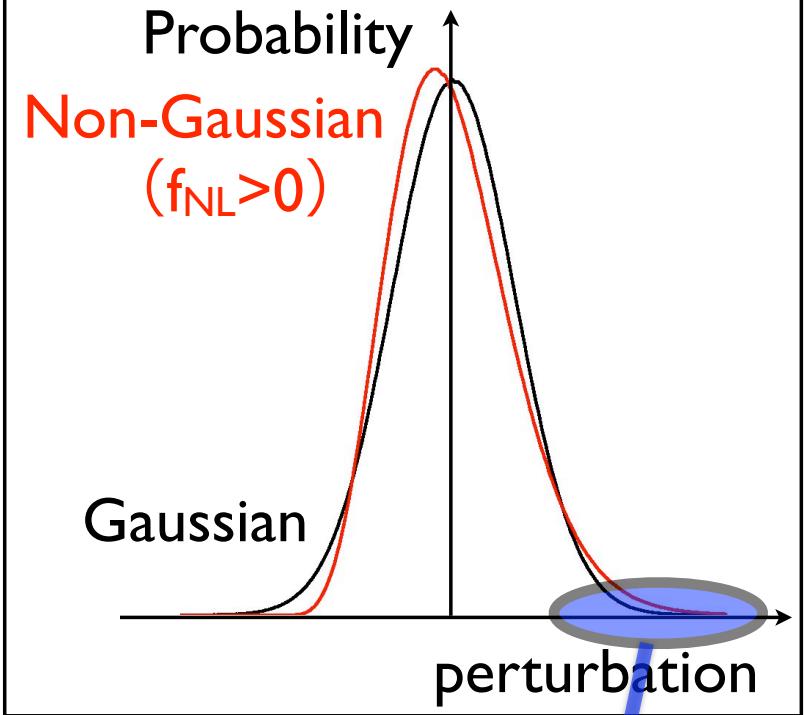
Gaussian $-10 < f_{nl} < 74$ (95% CL) WMAP7(Komatsu+10)

We observe ``galaxy'',
not ``matter'' density fluctuations

biasing changes things dramatically!

- halo mass function
- halo power spectrum
- halo bispectrum

**Understanding of the halo/galaxy
biasing is the key!**



Scale-dependent bias

Theory

peak-background split
and/or peak(local) bias

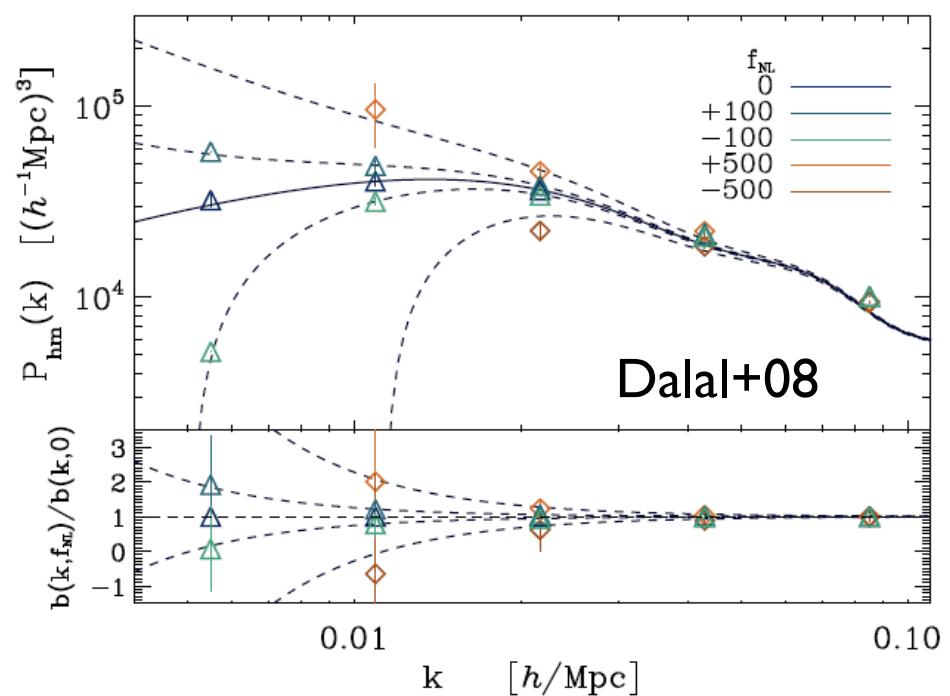
Dalal+08
Slosar+08
Matarrese,Verde08
Afshordi,Tolley08
McDonald08
Taruya+09
Giannantonio,Porciani10
Desjacques,Jeong,Schmidt11a,b
and more ...

calibration by simulations

Desjacques+09
Grossi+09
Pillepich+10

Slosar+08

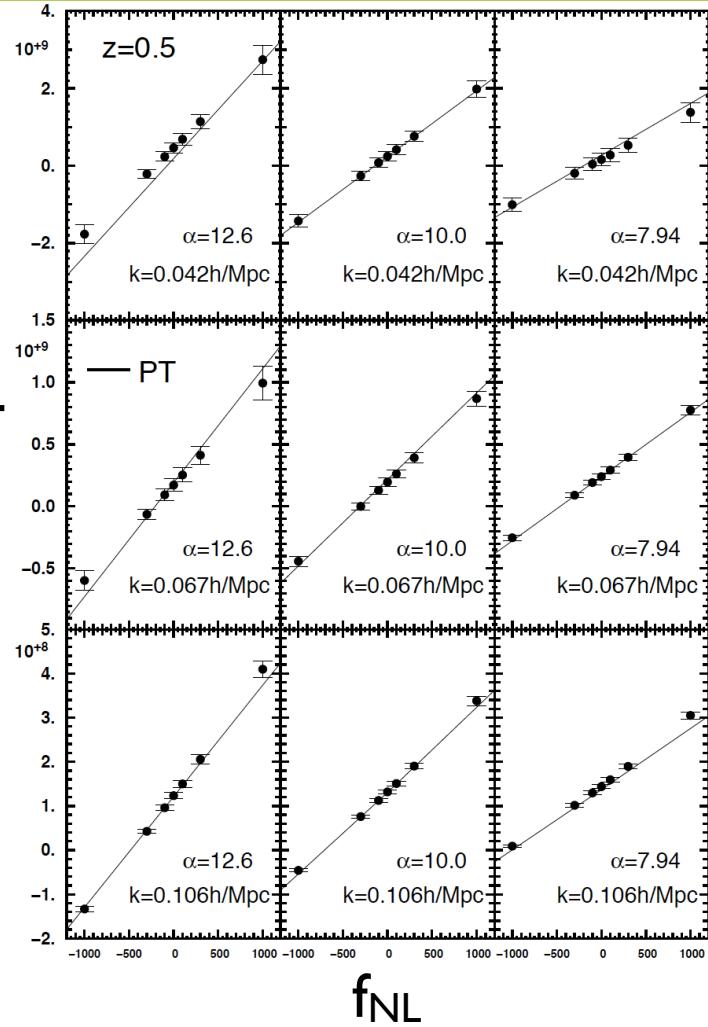
$-29 < f_{\text{nl}} < 69$ (QSOs+more)



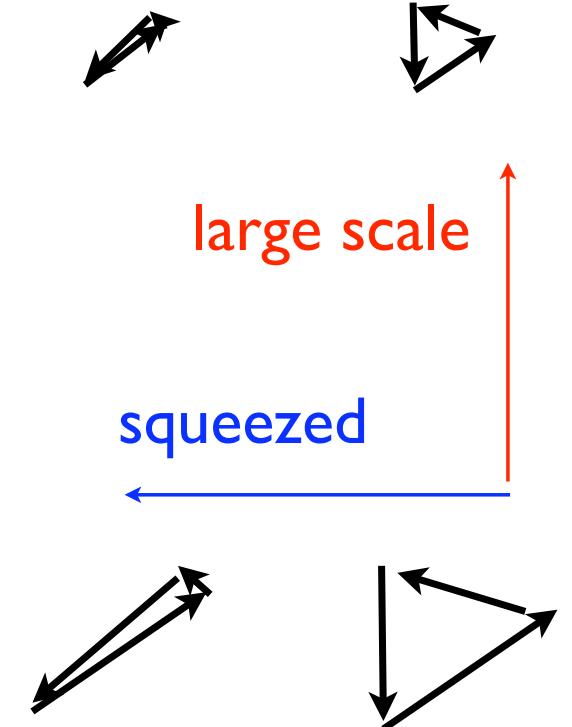
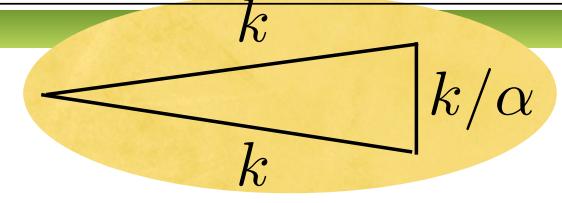
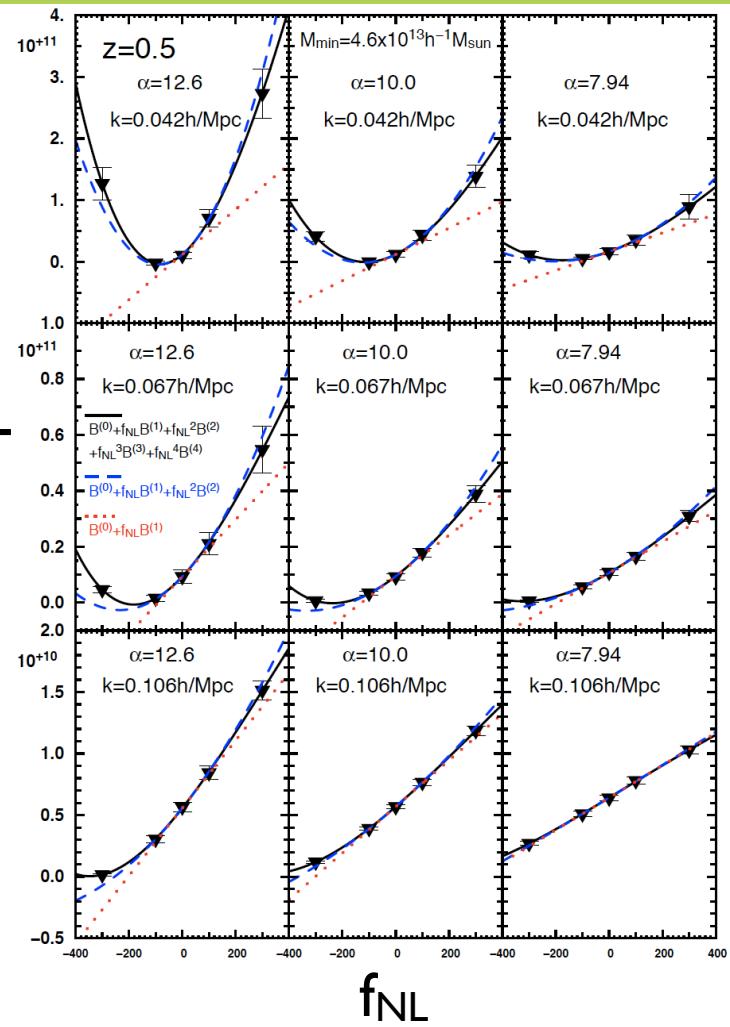
signature of f_{NL} in bispectrum

TN, Taruya, Koyama & Sabiu '10

Matter bispectrum



Halo bispectrum



Peak-Background Split prediction

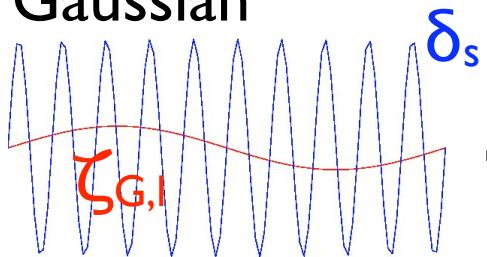
peak-background split

$$\zeta_G = \zeta_{G,\ell} + \zeta_{G,s}$$

$$\delta = \delta_\ell + \delta_s$$

responsible for halo formation

Gaussian



non-Gaussian

$$\delta_h(\mathbf{x}) = \sum_{m,n} \frac{b_{mn}}{m!n!} \delta^m(\mathbf{x}) \zeta_G^n(\mathbf{x})$$

Giannantonio, Porciani 10

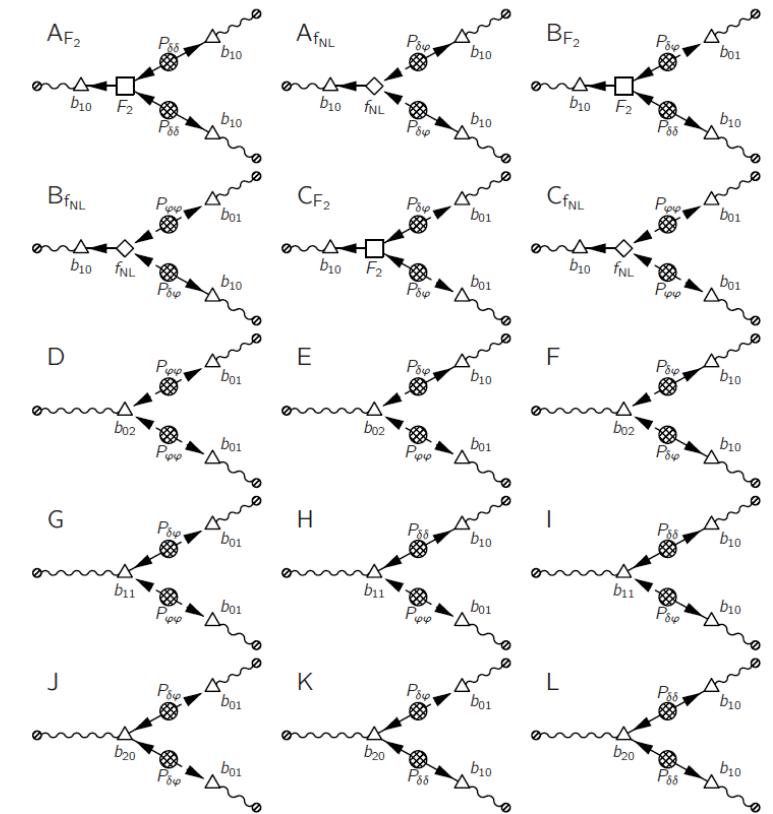
coefficients b_{mn} are given as derivatives of mass function

power spectrum

$$P_h(k) = b_{10}^2 P_\delta(k) + 2b_{10}b_{01}P_{\delta\zeta}(k) + b_{01}^2 P_\zeta(k)$$

bispectrum

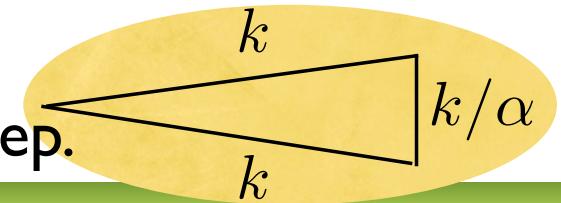
Baldauf, Seljak & Senatore'10



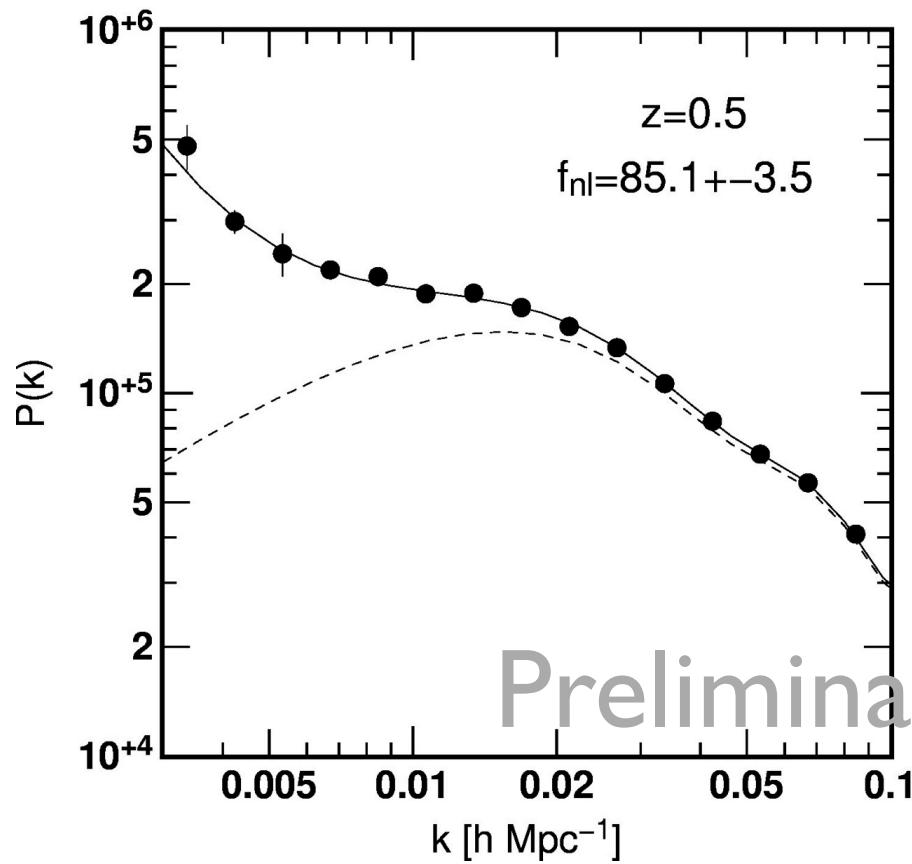
relevant bias parameters: $b_{10}, b_{01}, b_{20}, b_{11}, b_{02}$

recovery of f_{nl} ?

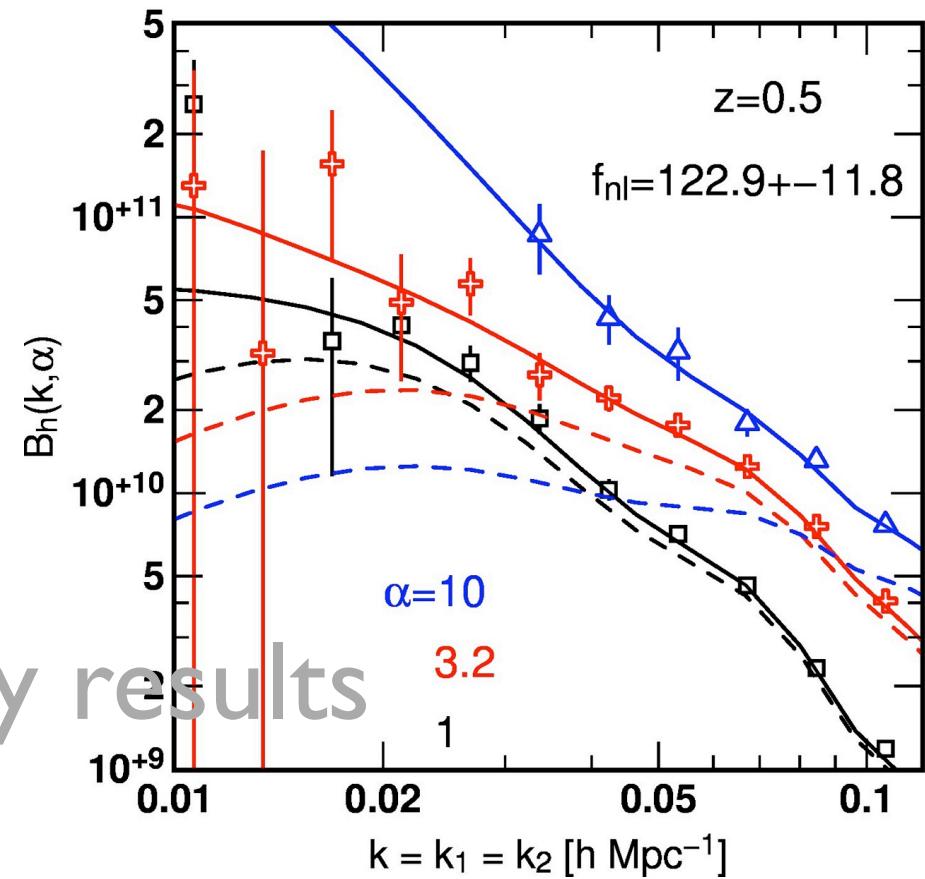
TN in prep.



power spectrum



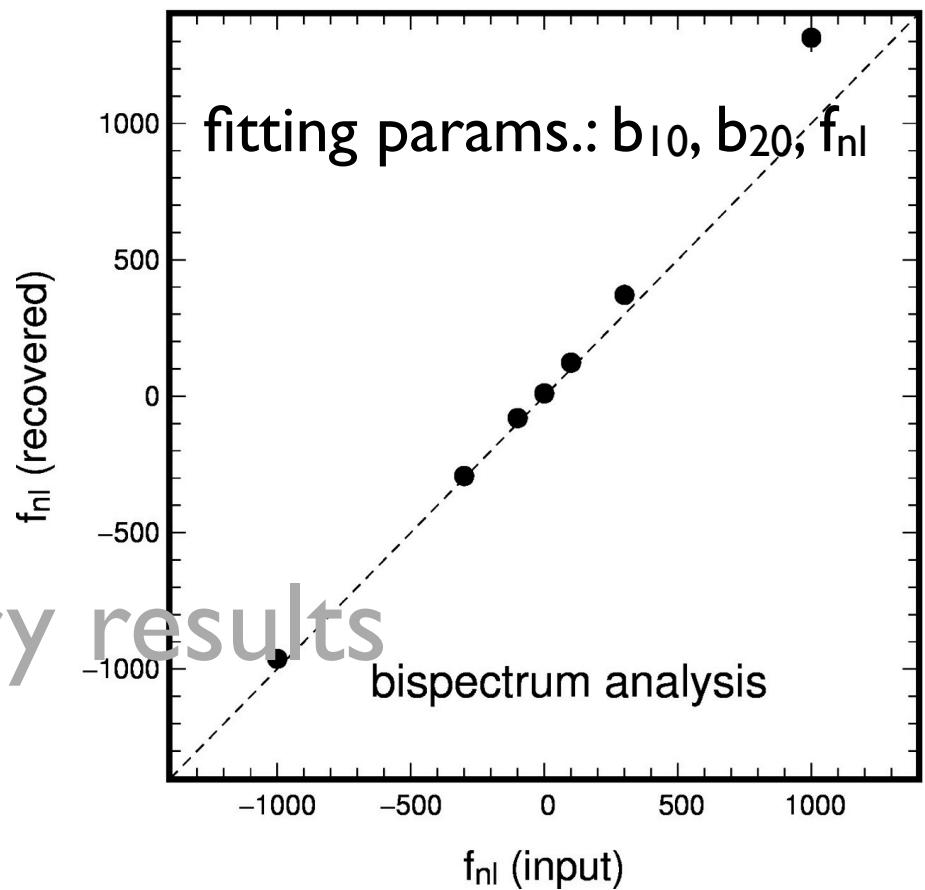
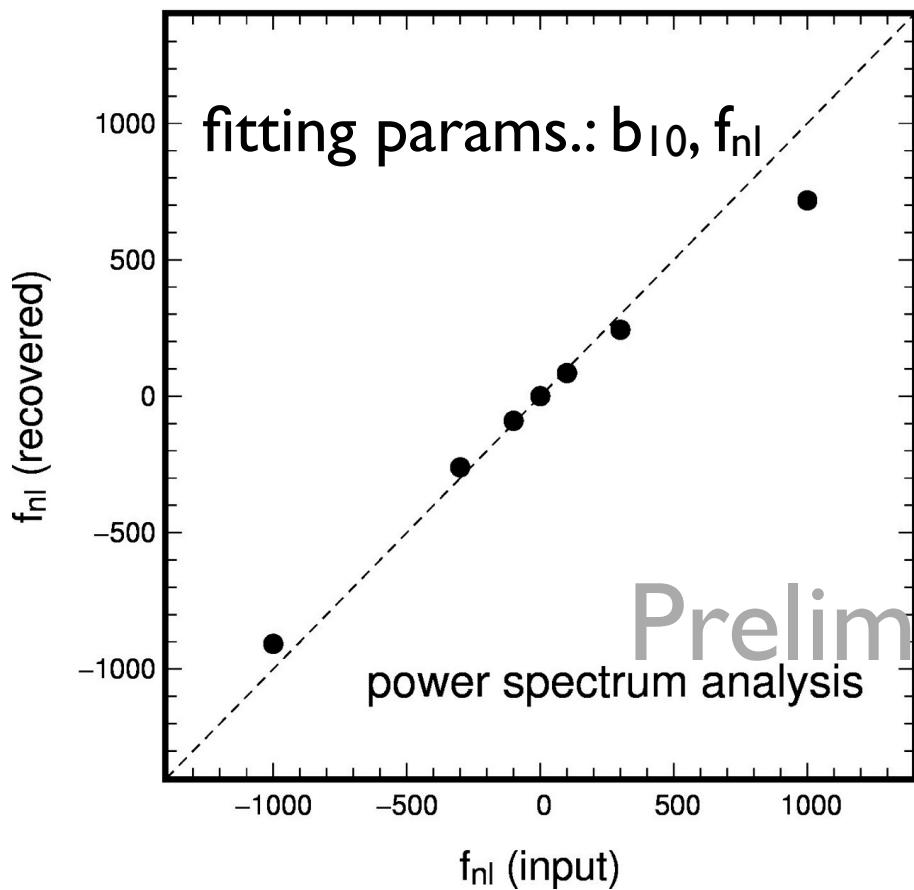
bispectrum



Preliminary results

recovery of f_{nl} ?

TN in prep.



Preliminary results

multi-field nG?

① local-type scale-independent nG

TN in prep.

- What we observe in halo clustering when **Bispectrum & Trispectrum** exist at the beginning?
- We already have both **B** & **T** in $\Phi = \varphi + f_{\text{nl}} \varphi^2$ $\tau_{\text{nl}} = (36/25) f_{\text{nl}}^2$
- (scale-independent) local models are parametrized by $(f_{\text{nl}}, g_{\text{nl}}, \tau_{\text{nl}})$ in general

$$B_\zeta(k_1, k_2, k_3) = \frac{6}{5} f_{\text{nl}} [P_\zeta(k_1) P_\zeta(k_2) + (\text{perm.})], \quad \tau_{\text{nl}} \geq (36/25) f_{\text{nl}}^2$$

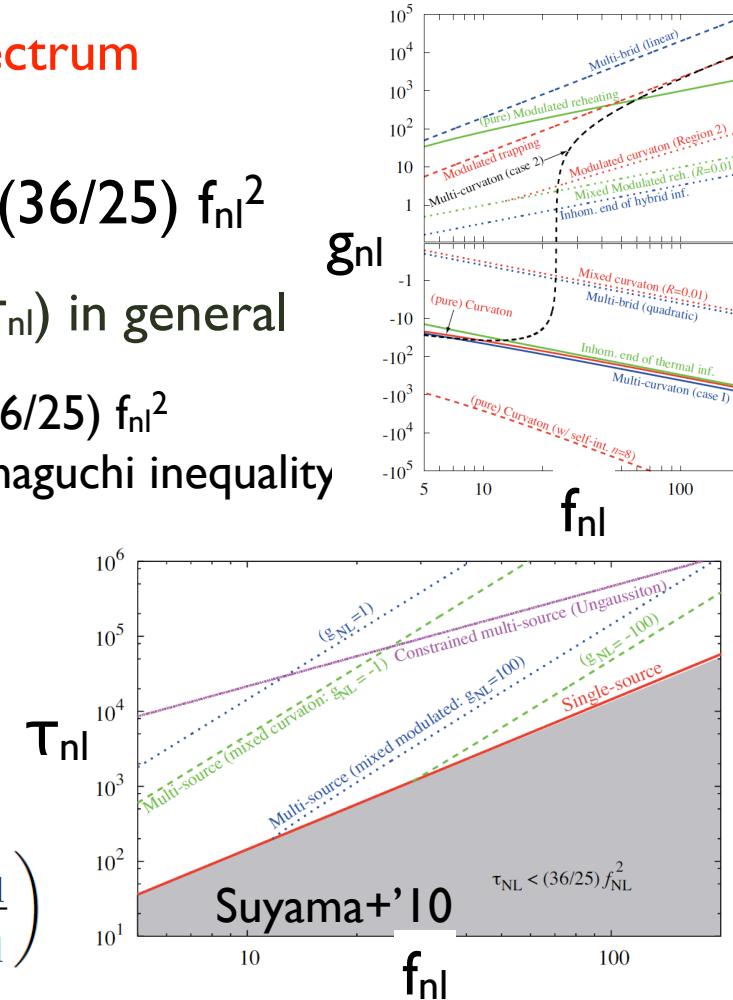
$$T_\zeta(k_1, k_2, k_3, k_4) = \tau_{\text{nl}} [P_\zeta(k_{13}) P_\zeta(k_3) P_\zeta(k_4) + (\text{perm.})] \text{ Suyama-Yamaguchi inequality}$$

$$+ \frac{54}{25} g_{\text{nl}} [P_\zeta(k_2) P_\zeta(k_3) P_\zeta(k_4) + (\text{perm.})].$$

- This can be realized by employing 2 Gaussian fields:

$$\zeta(\mathbf{x}) = \chi_1(\mathbf{x}) + \chi_2(\mathbf{x}) + \widetilde{f_{\text{nl}}} [\chi_2^2(\mathbf{x}) - \langle \chi_2^2 \rangle] + \widetilde{g_{\text{nl}}} \chi_2^3(\mathbf{x})$$

$$P_{\chi_1}(k) = (1 - \alpha) P_\zeta(k) \quad \left(\widetilde{f_{\text{nl}}}, \widetilde{g_{\text{nl}}}, \alpha \right) = \left(\frac{125}{432} \frac{\tau_{\text{nl}}^2}{f_{\text{nl}}^3}, \frac{625}{5184} \frac{\tau_{\text{nl}}^3}{f_{\text{nl}}^6} g_{\text{nl}}, \frac{36}{25} \frac{f_{\text{nl}}^2}{\tau_{\text{nl}}} \right)$$



PBS prediction

- “long mode”, “short mode” decomposition for 2 Gaussian fields:

$$\chi_i = \chi_{i,\ell} + \chi_{i,s} \quad i = 1, 2$$

- “local” moments are modulated by long mode

$$\bar{\mu}_i(R) \equiv \langle \delta_s^i(R) \rangle_c \quad \mu_i(\mathbf{x}; R) \equiv \langle \delta_s^i(\mathbf{x}; R) \rangle_{c|\chi_{i,\ell}(\mathbf{x})}$$

variance

$$\mu_2 \simeq \bar{\mu}_2 \left[1 + 4 \tilde{f}_{\text{nl}} \alpha \chi_{2,\ell} \right] = \bar{\mu}_2 \left[1 + \frac{5}{3} \frac{\tau_{\text{nl}}}{f_{\text{nl}}} \underline{\chi_{2,\ell}} \right]$$

$$\mu_3 \simeq \bar{\mu}_3 + \Delta\mu_3,$$

skewness

$$\bar{\mu}_3 \equiv f_{\text{nl}} \hat{\mu}_3, \quad \text{See also Desjacques,Jeong,Schmidt'11}$$

$$\Delta\mu_3 \equiv \frac{1}{60} \left(\frac{25\tau_{\text{nl}}}{36f_{\text{nl}}^2} \right) (27g_{\text{nl}} + 25\tau_{\text{nl}}) \hat{\mu}_3 \underline{\chi_{2,\ell}}$$

$$\delta_h^L = \frac{f(\mu_2, \mu_3, \dots; \delta_c - \delta_\ell)}{f(\bar{\mu}_2, \bar{\mu}_3, \dots; \delta_c)} - 1$$

$$b_\delta = 1 - \frac{\partial \ln f}{\partial \delta_c}$$

$$\delta_h = b_\delta \delta + b_{\chi_2} \chi_2$$

$$b_{\chi_2} = \sum_{i=2}^{\infty} \frac{\partial \ln f}{\partial \mu_i} \frac{\partial \mu_i}{\partial \chi_{2,\ell}},$$

$$= \frac{5}{3} \frac{\tau_{\text{nl}}}{f_{\text{nl}}} \bar{\mu}_2 \frac{\partial \ln f}{\partial \mu_2} + \frac{1}{60} \left(\frac{25}{36} \frac{\tau_{\text{nl}}}{f_{\text{nl}}^2} \right) (27g_{\text{nl}} + 25\tau_{\text{nl}}) \hat{\mu}_3 \frac{\partial \ln f}{\partial \mu_3} + \dots$$

final expression

$$\begin{aligned} P_h(k) = & b_\delta^2 P_\delta(k) + \left[\frac{12}{5} f_{\text{nl}} \delta_c b_\delta (b_\delta - 1) + \frac{1}{30} (27g_{\text{nl}} + 25\tau_{\text{nl}}) b_\delta \hat{\mu}_3 \frac{\partial \ln f}{\partial \mu_3} \right] P_{\delta\zeta}(k) \\ & + \left[\tau_{\text{nl}} \delta_c^2 (b_\delta - 1)^2 + \frac{\tau_{\text{nl}}}{f_{\text{nl}}} \left(\frac{27g_{\text{nl}} + 25\tau_{\text{nl}}}{72} \hat{\mu}_3 \frac{\partial \ln f}{\partial \mu_3} \right)^2 \right] P_\zeta(k) \end{aligned}$$

N-body simulations and analysis

- $N=1024^3$ particles in a $L=4096\text{Mpc}/h$ box
- 2LPT @ $z=19 \rightarrow$ output @ $z=1$
- $f_{\text{nl}}=100, \tau_{\text{nl}}=(36/25)f_{\text{nl}}^2$
- $f_{\text{nl}}=100, \tau_{\text{nl}}=2\times(36/25)f_{\text{nl}}^2$
- $g_{\text{nl}}=1\times10^6$

$$\delta_h = b_\delta \delta + b_{\chi_2} \chi_2$$

$$\delta_h = b_\delta \mathcal{M}(k) \chi_1 + [b_\delta \mathcal{M}(k) + b_{\chi_2}] \chi_2$$

“propagator”

$$\langle \delta_h(\mathbf{k}) \chi_i(\mathbf{k}') \rangle = \mathcal{M}_{i \rightarrow h}(k) \langle \chi_i(\mathbf{k}) \chi_i(\mathbf{k}') \rangle$$

at lowest order: $\mathcal{M}_{1 \rightarrow h}(k) = b_\delta \mathcal{M}(k),$
 $\mathcal{M}_{2 \rightarrow h}(k) = b_\delta \mathcal{M}(k) + b_{\chi_2}$

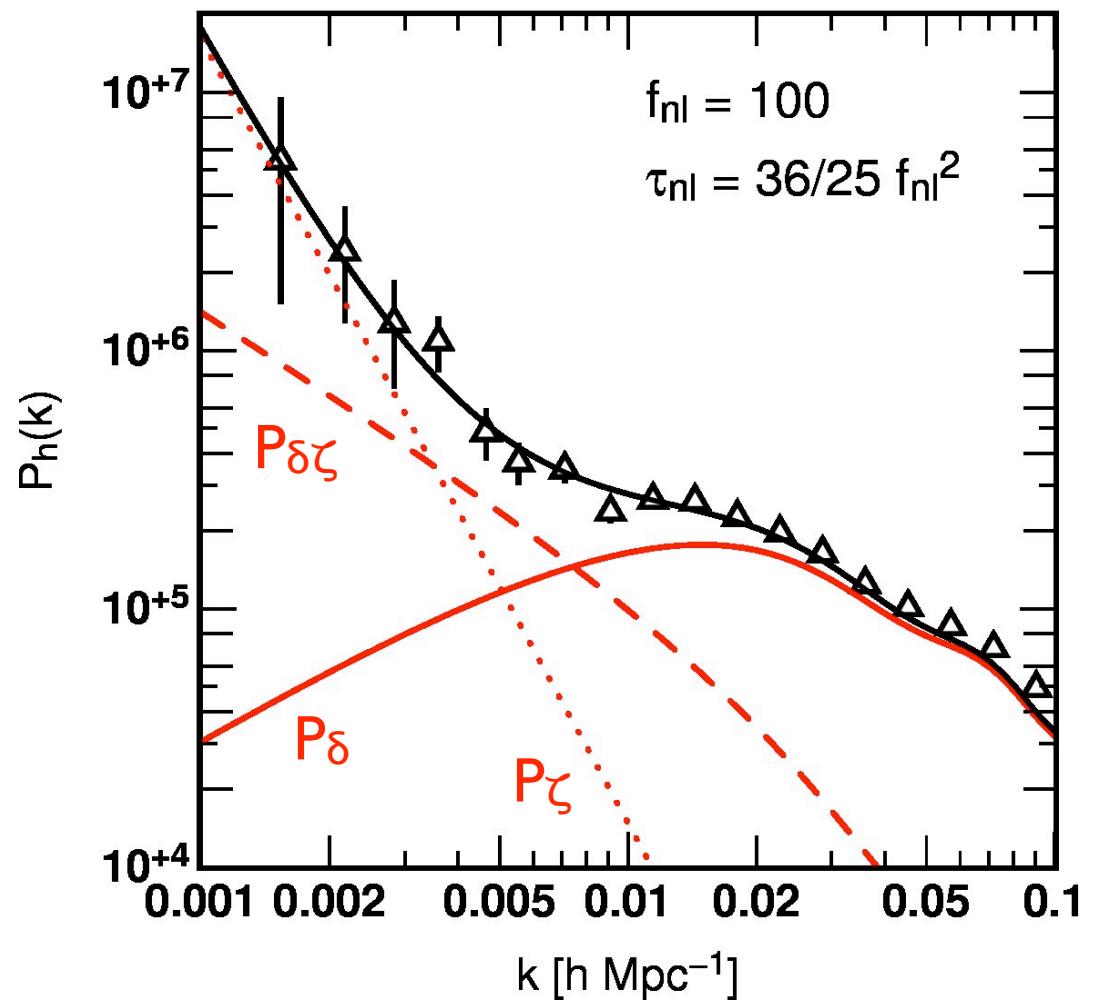
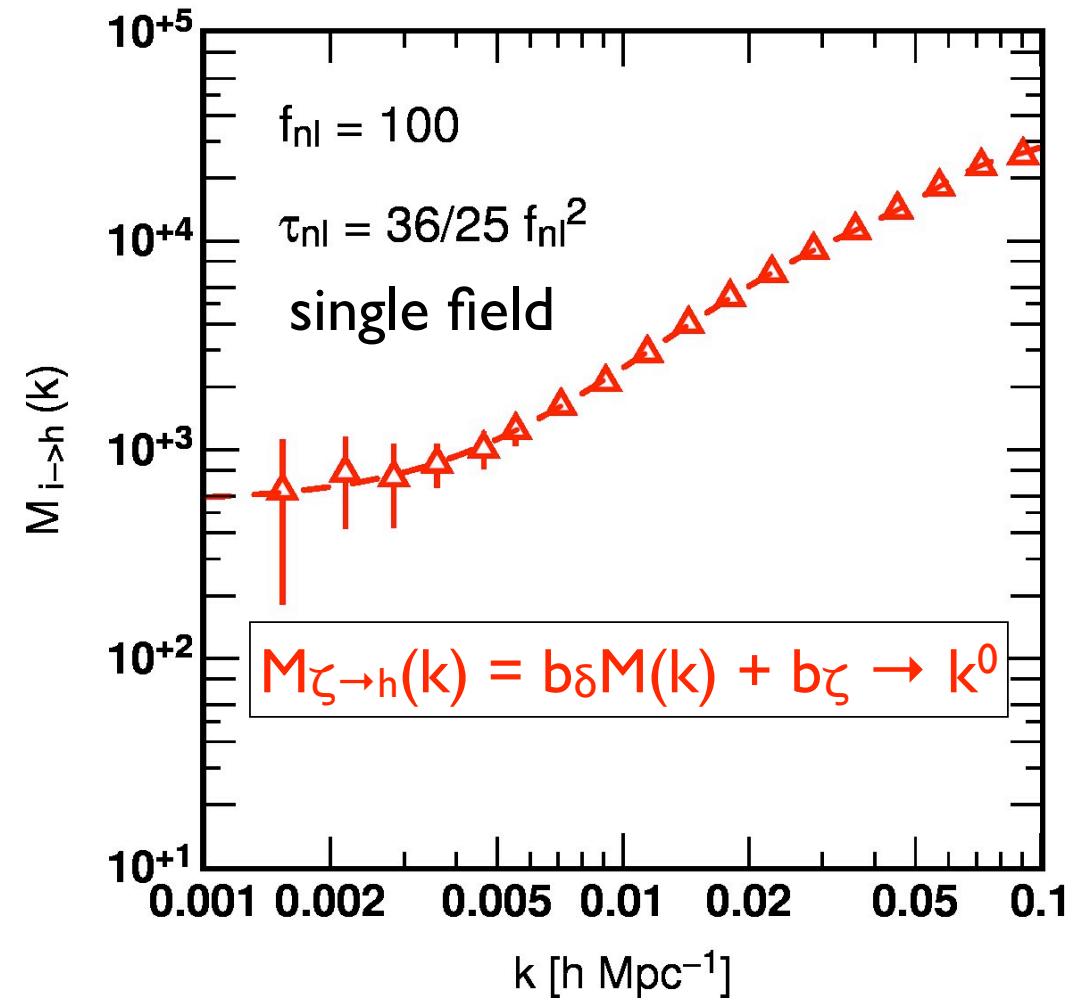
2 fitting params

c.f., matter transfer function

$$\delta(\mathbf{k}) = \mathcal{M}(k) \zeta(\mathbf{k}) \propto k^2 T(k) \zeta(\mathbf{k})$$

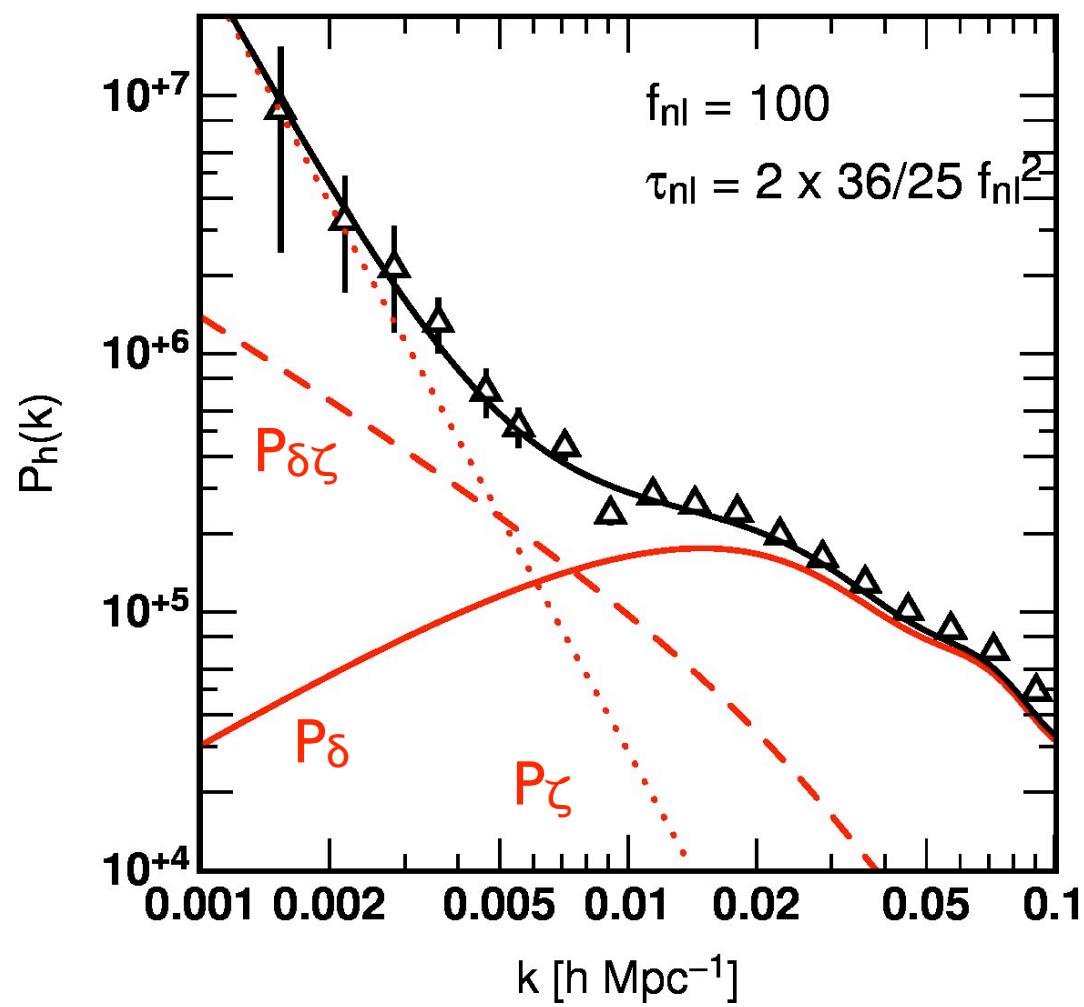
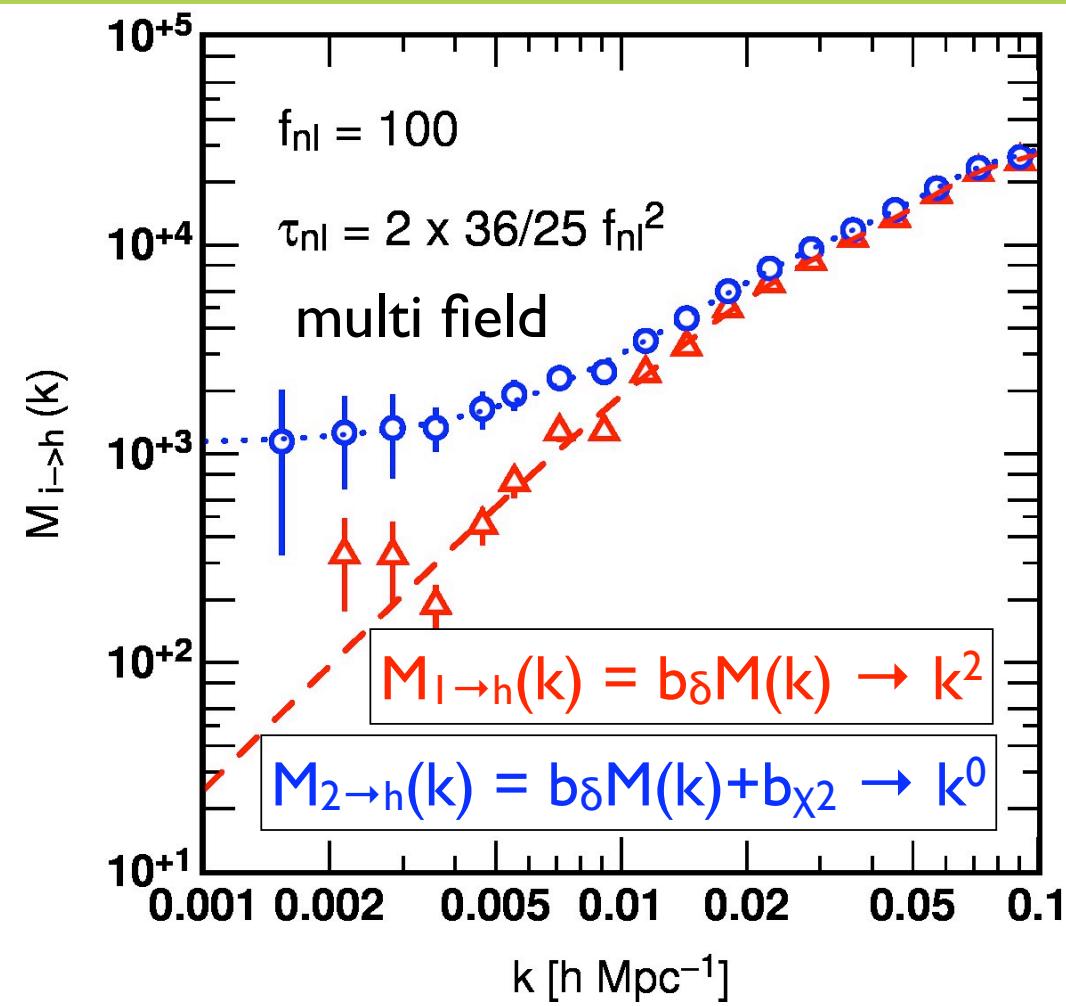
$f_{nl} + \tau_{nl}$

$$P_h(k) = b_\delta^2 P_\delta(k) + \frac{12}{5} f_{nl} \delta_c b_\delta (b_\delta - 1) P_{\delta\zeta}(k) + \tau_{nl} \delta_c^2 (b_\delta - 1)^2 P_\zeta(k)$$



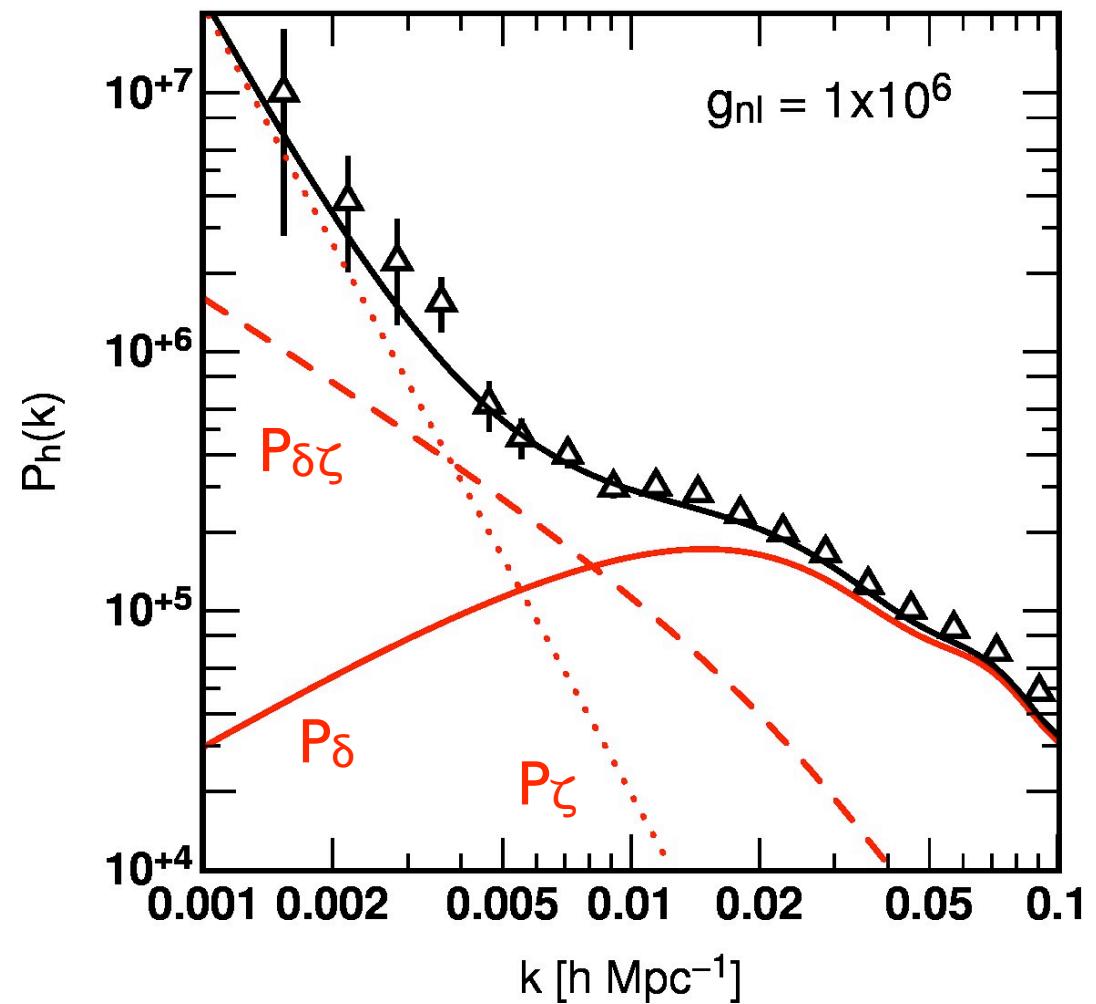
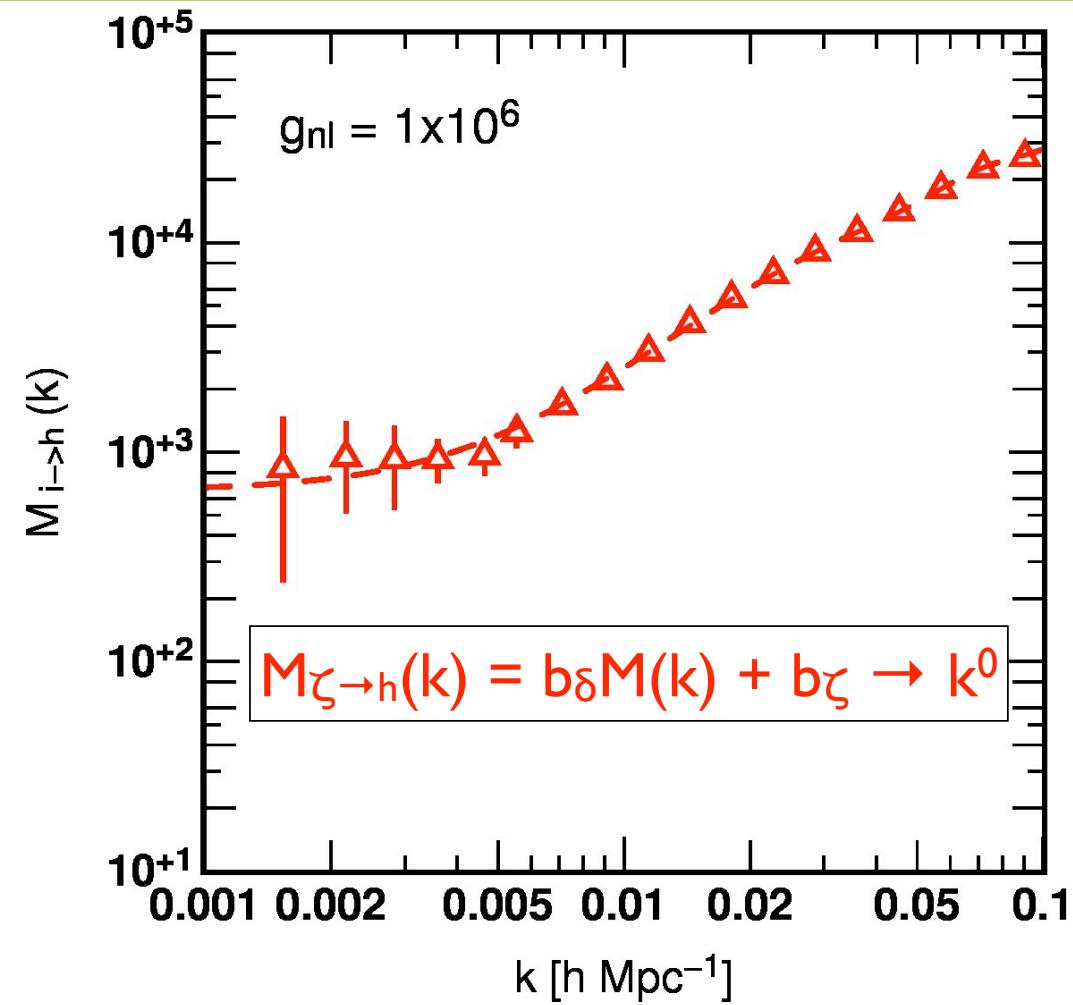
f_{nl} + τ_{nl}

$$P_h(k) = b_\delta^2 P_\delta(k) + \frac{12}{5} f_{nl} \delta_c b_\delta (b_\delta - 1) P_{\delta\zeta}(k) + \tau_{nl} \delta_c^2 (b_\delta - 1)^2 P_\zeta(k)$$

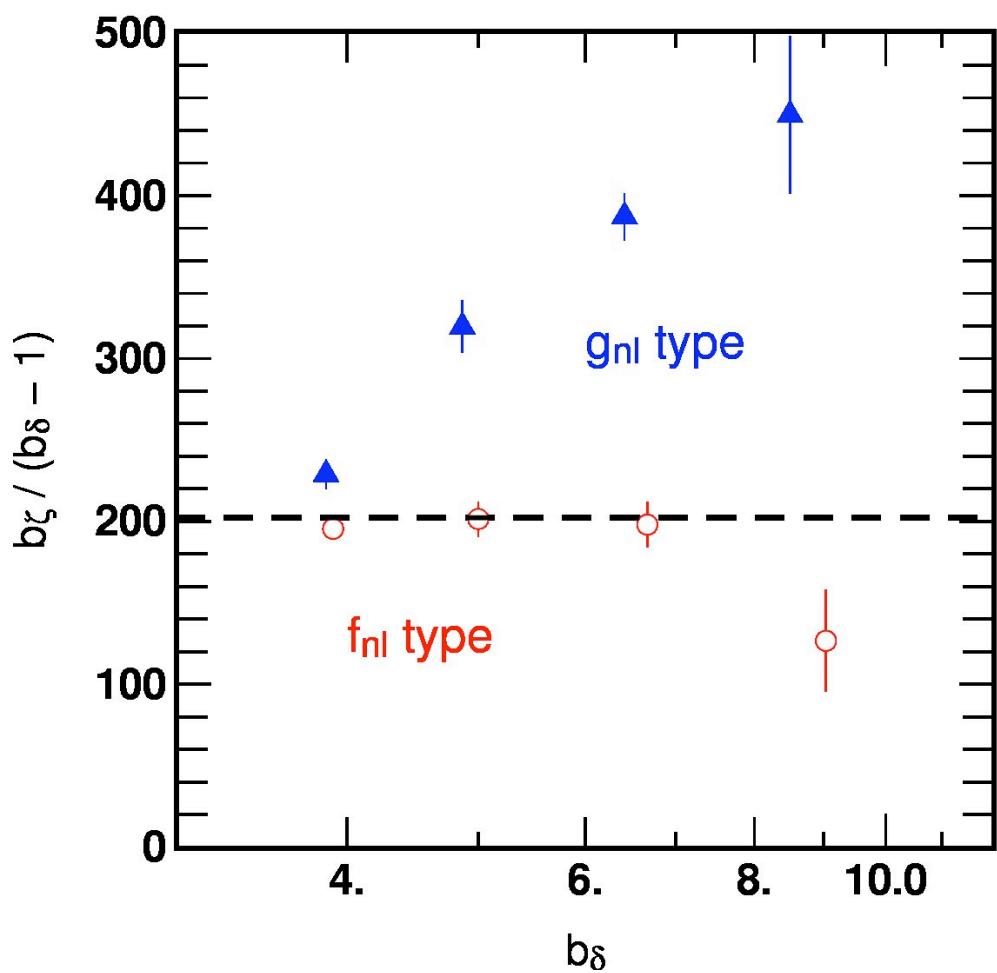


g_{nl}

$$P_h(k) = b_\delta^2 P_\delta(k) + \frac{9}{10} g_{nl} b_\delta \hat{\mu}_3 \frac{\partial \ln f}{\partial \mu_3} P_{\delta\zeta}(k) + \left[\frac{9}{20} g_{nl} \hat{\mu}_3 \frac{\partial \ln f}{\partial \mu_3} \right]^2 P_\zeta(k)$$



f_{nl} ? g_{nl} ? Mass dependence



- halo P(k) shows the same k -dependence in f_{nl} model and g_{nl} model.
 - the nG correction comes from different origins
 - f_{nl} : modulation in the *local variance*
- $$b_\zeta = \frac{12}{5} f_{\text{nl}} \bar{\mu}_2 \frac{\partial \ln f}{\partial \mu_2} = \frac{6}{5} f_{\text{nl}} \delta_c (b_\delta - 1)$$
- assume universal mass function
- g_{nl} : modulation in the *local skewness*
- $$b_\zeta = \frac{9}{20} g_{\text{nl}} \hat{\mu}_3 \frac{\partial \ln f}{\partial \mu_3}$$
- Detection of nG signal from different tracers is a key to distinguish the 2 models

② local-type scale-dependent nG

TN Taruya Koyama in prep.

- Observation indicates an almost Gaussian almost adiabatic initial condition
→ (Perfectly) Gaussian adiabatic field + (strongly) non-Gaussian non-adiabatic field ?
- More general 2 field local-type nG: $\delta(\mathbf{k}) = \mathcal{M}_1(k)X_1(\mathbf{k}) + \mathcal{M}_2(k)X_2(\mathbf{k})$

field 1

$$\begin{aligned} X_1 &= \chi_1 \\ \mathcal{M}_1(k) &= \mathcal{M}_{\text{adi}}(k) \\ \frac{k^3}{2\pi^2} P_{\chi_1}(k) &= A_{\chi_1} \left(\frac{k}{k_0} \right)^{n_{\chi_1}-1} \end{aligned}$$

field 2

$$\begin{aligned} X_2(\mathbf{x}) &= \chi_2(\mathbf{x}) + \widetilde{f}_{\text{nl}} \left[\chi_2^2(\mathbf{x}) - \langle \chi_2^2 \rangle \right] \\ \mathcal{M}_2 &= \mathcal{M}_{\text{adi}} \quad \text{or} \quad \mathcal{M}_2 = \mathcal{M}_{\text{iso}} \\ \frac{k^3}{2\pi^2} P_{\chi_2}(k) &= A_{\chi_2} \left(\frac{k}{k_0} \right)^{n_{\chi_2}-1} \end{aligned}$$

cross correlation

$$\beta \equiv -\frac{P_{\chi_1\chi_2}(k)}{P_{\chi_1}(k)P_{\chi_2}(k)}$$

- parameters: A_{χ_1} , n_{χ_1} , A_{χ_2} , n_{χ_2} , $\widetilde{f}_{\text{nl}}$, β , transfer function of X_2

PBS prediction

- “long mode”, “short mode” decomposition for 2 Gaussian fields:

$$\chi_i = \chi_{i,\ell} + \chi_{i,s} \quad i = 1, 2$$

- “local” moments are modulated by long mode

$$\bar{\mu}_i \equiv \langle \delta^i(R) \rangle_c \quad \mu_i(\mathbf{x}) \equiv \langle \delta^i(\mathbf{x}; R) \rangle_c$$

variance

$$\mu_2 \simeq \bar{\mu}_2 \left[1 + 4 \frac{\sigma_{12}^2 + \sigma_2^2}{\sigma^2} \underline{\chi_{2,\ell}} \right]$$

$$\sigma^2 \equiv \bar{\mu}_2 \equiv \sigma_1^2 + 2\sigma_{12}^2 + \sigma_2^2$$

$$\sigma_i^2 \equiv \langle (\mathcal{M}_i * \chi_{i,s})^2 \rangle,$$

$$\sigma_{12}^2 \equiv \langle (\mathcal{M}_1 * \chi_{1,s})(\mathcal{M}_2 * \chi_{2,s}) \rangle$$

$$\delta_h^L = \frac{f(\mu_2, \cancel{\mu_3}, \dots; \delta_c - \delta_\ell)}{f(\bar{\mu}_2, \cancel{\bar{\mu}_3}, \dots; \delta_c)} - 1$$

$$\delta_h = b_\delta \delta + b_{\chi_2} \chi_2$$

$$b_\delta = 1 - \frac{\partial \ln f}{\partial \delta_c}$$

$$b_{\chi_2} = 2 \tilde{f}_{nl} \frac{\sigma_{12}^2 + \sigma_2^2}{\sigma^2} \delta_c [b_\delta - 1]$$

final expression

$$\begin{aligned} P_h(k) &= b_\delta^2 M_1^2(k) P_{\chi_1}(k) + 2 b_\delta M_1(k) [b_\delta M_2(k) + b_{\chi_2}] P_{\chi_1 \chi_2}(k) \\ &\quad + [b_\delta M_2(k) + b_{\chi_2}]^2 P_{\chi_2}(k), \end{aligned}$$

N-body simulations and analysis

- $N=1024^3$ particles in a $L=4096 \text{Mpc}/h$ box
- 2LPT @ $z=19 \rightarrow$ output @ $z=1$
- $n_{\chi_2} = 1.5$
- $M_2(k) = M_{\text{iso}}(k)$ (CDM isocurvature)
- $\beta = -1$

$$\delta_h = b_\delta \delta + b_{\chi_2} \chi_2$$

$$\delta_h = b_\delta \mathcal{M}(k) \chi_1 + [b_\delta \mathcal{M}(k) + b_{\chi_2}] \chi_2$$

“propagator”

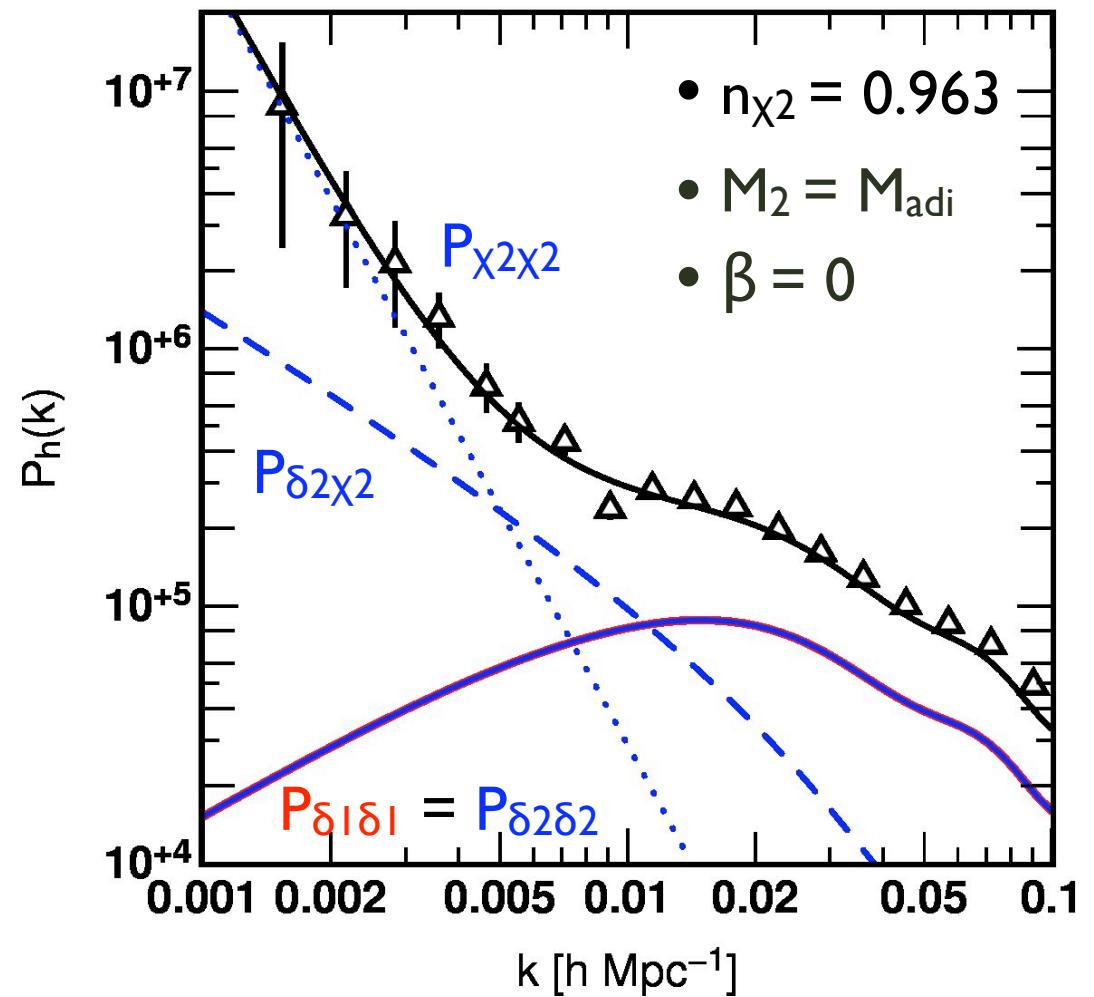
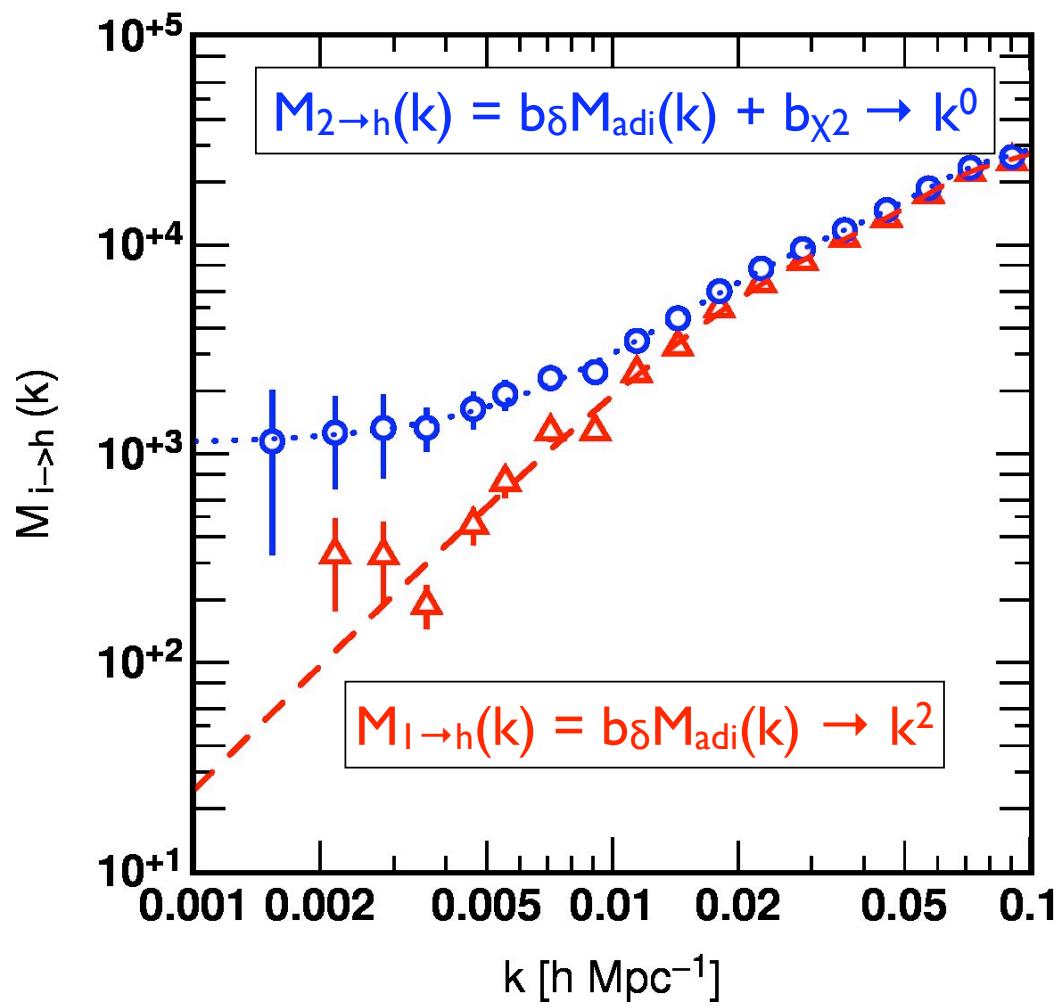
$$\langle \delta_h(\mathbf{k}) \chi_i(\mathbf{k}') \rangle = \mathcal{M}_{i \rightarrow h}(k) \langle \chi_i(\mathbf{k}) \chi_i(\mathbf{k}') \rangle$$

at lowest order: $\mathcal{M}_{1 \rightarrow h}(k) = b_\delta \mathcal{M}(k),$
 $\mathcal{M}_{2 \rightarrow h}(k) = b_\delta \mathcal{M}(k) + b_{\chi_2}$

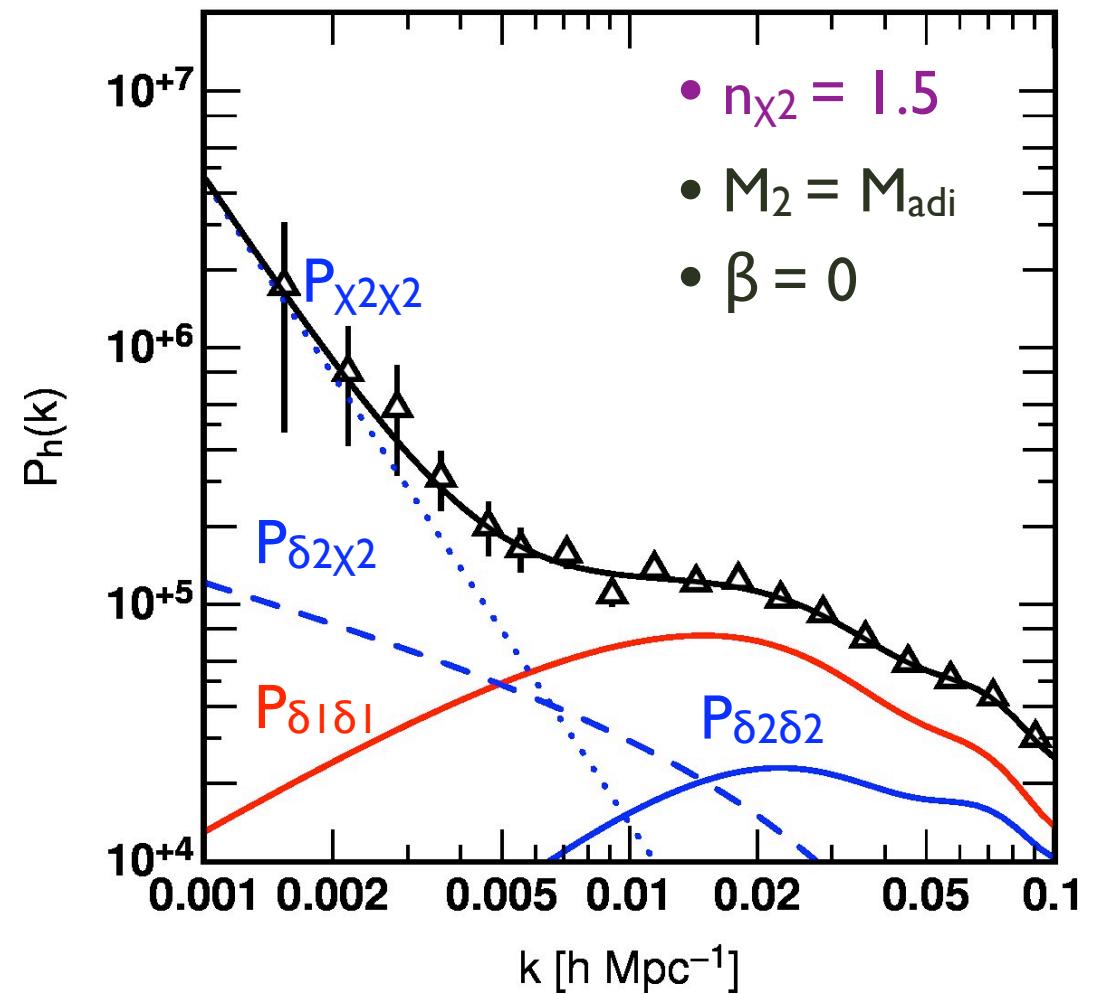
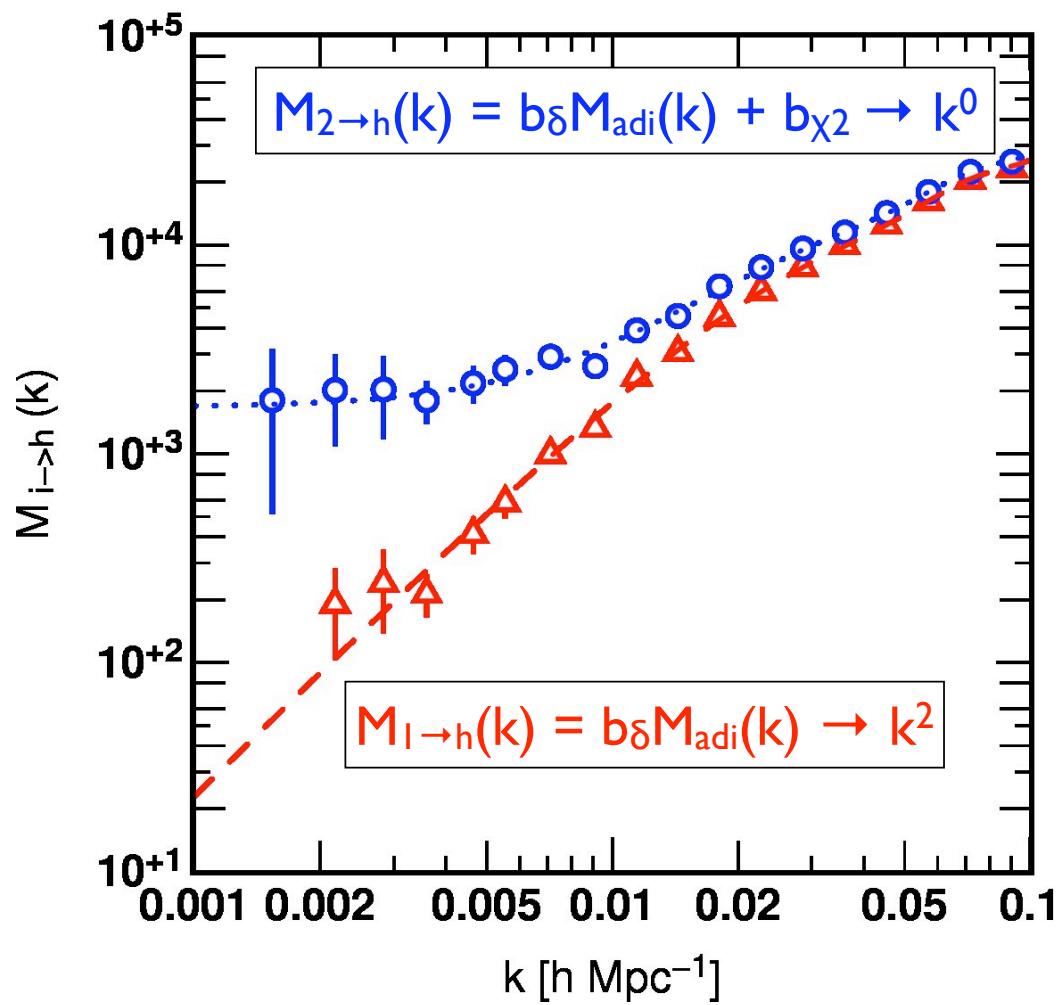
c.f., matter transfer function

$$\delta(\mathbf{k}) = \mathcal{M}(k) \zeta(\mathbf{k}) \propto k^2 T(k) \zeta(\mathbf{k})$$

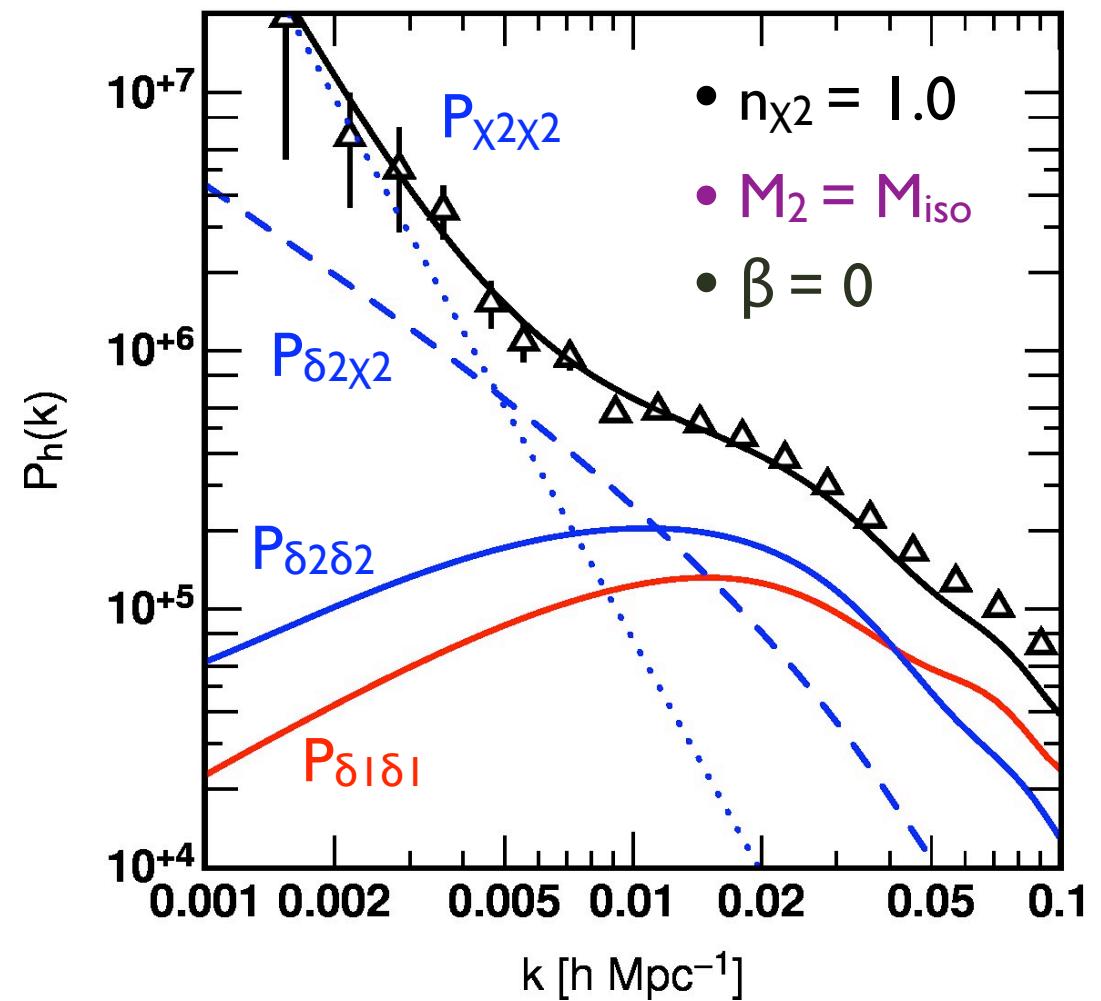
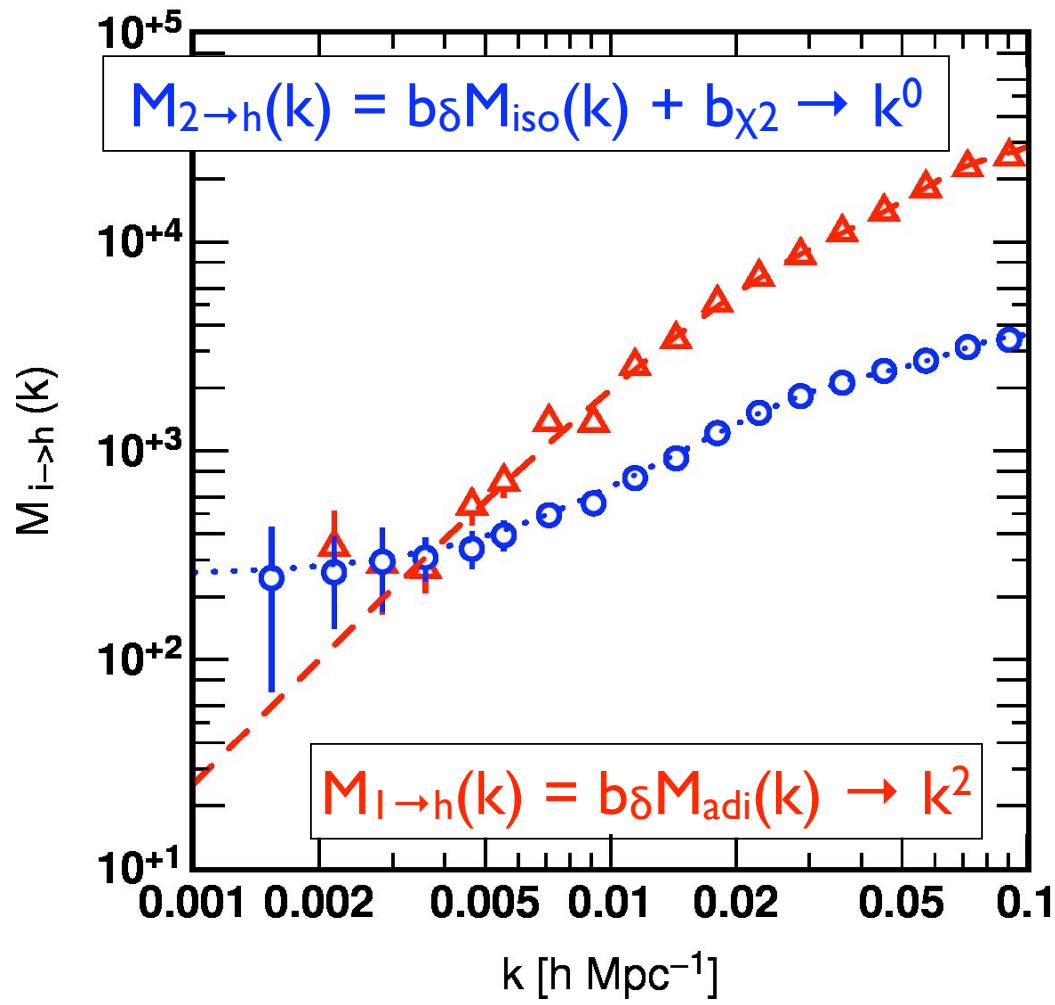
scale-independent nG



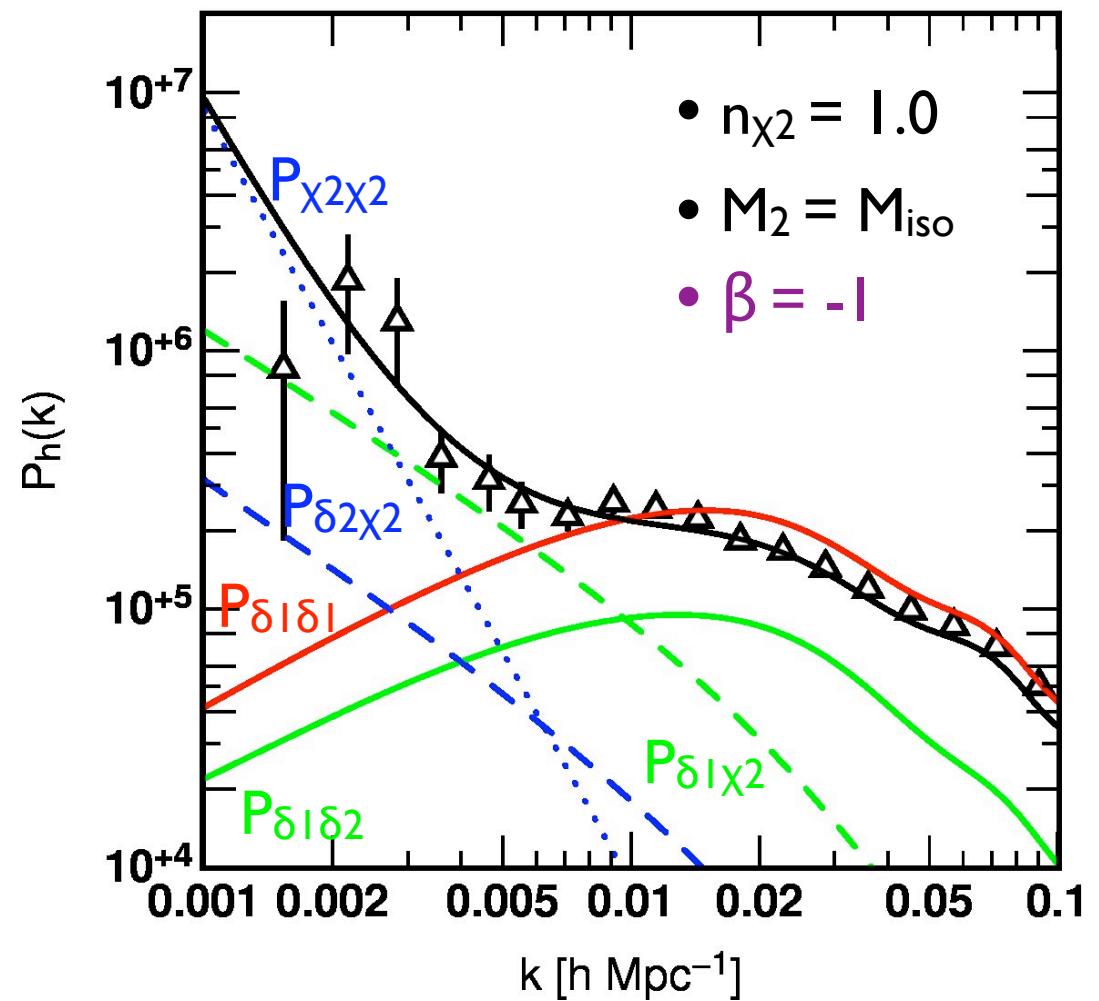
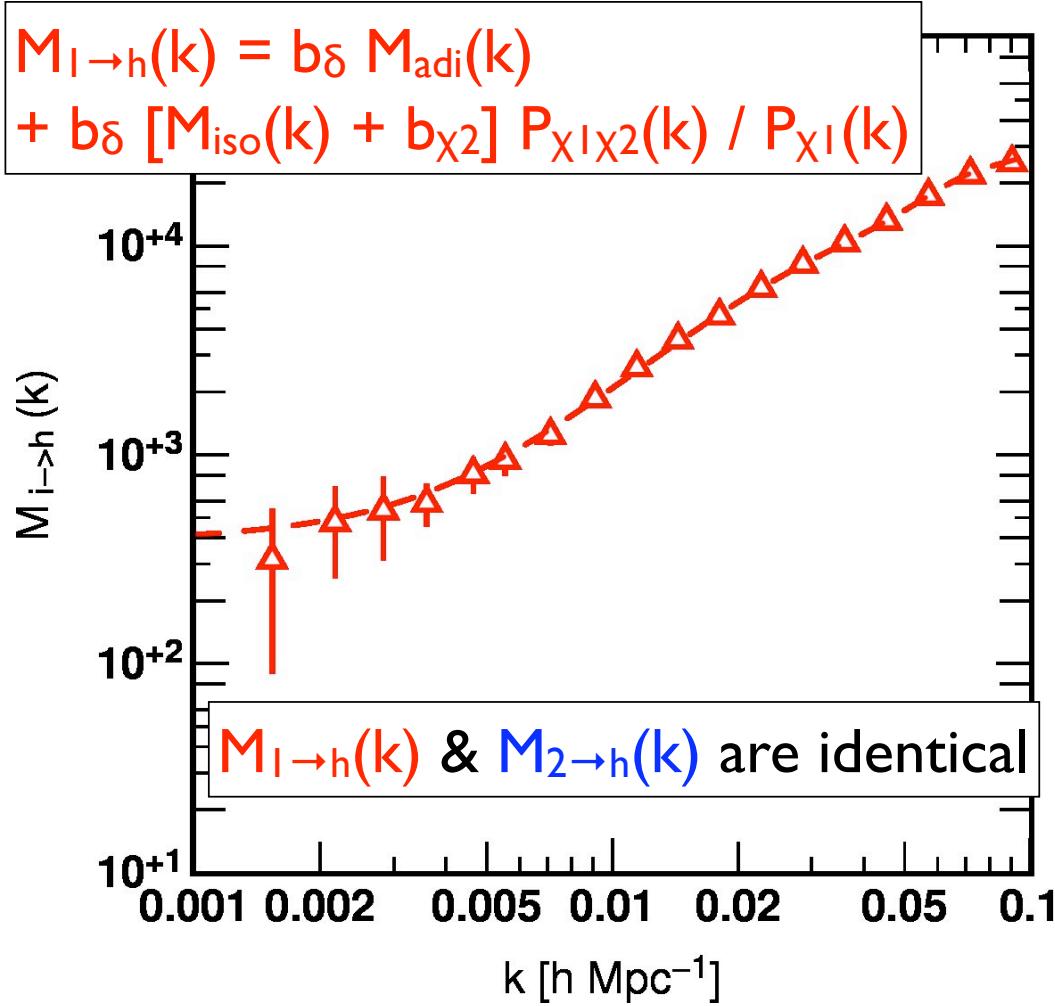
Effect of scalar spectral index



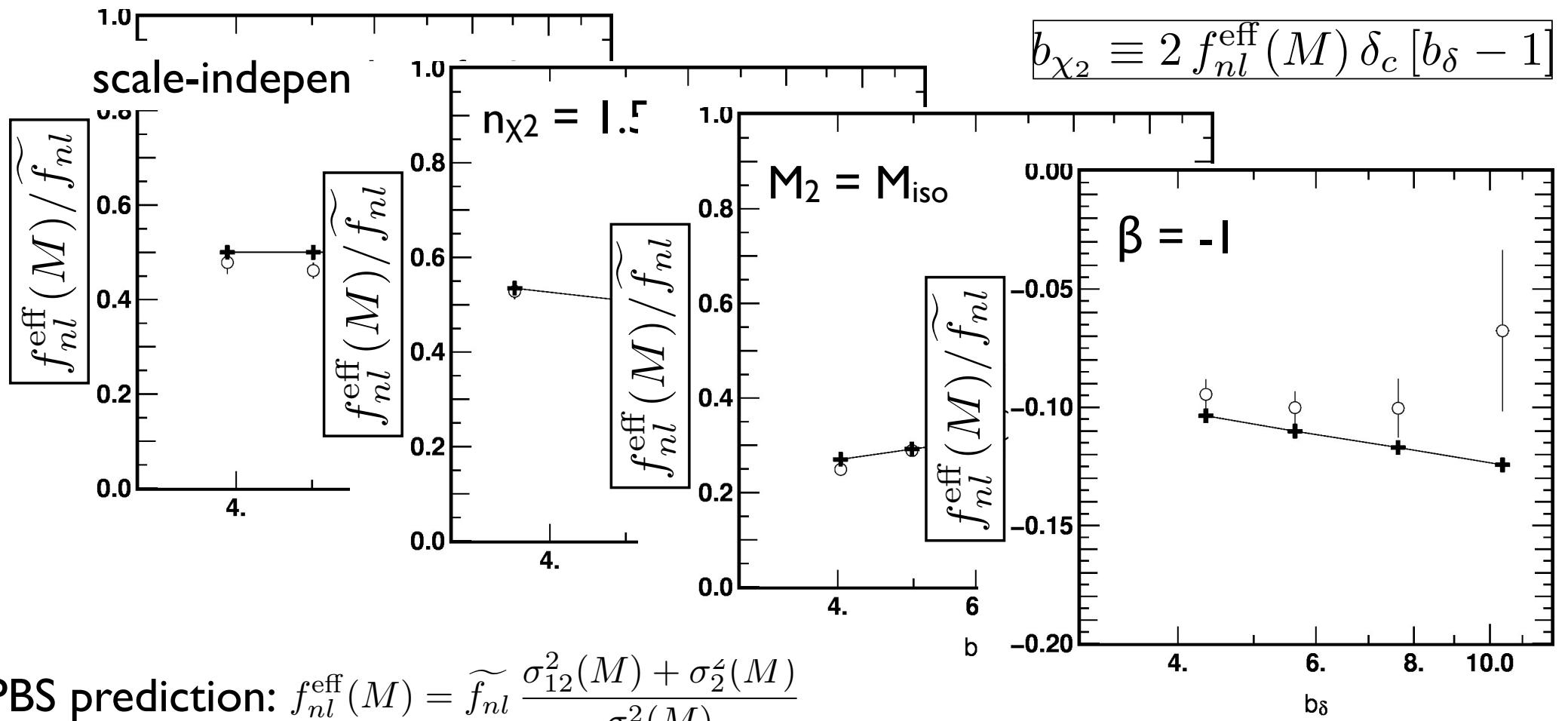
Effect of transfer function



Effect of cross correlation

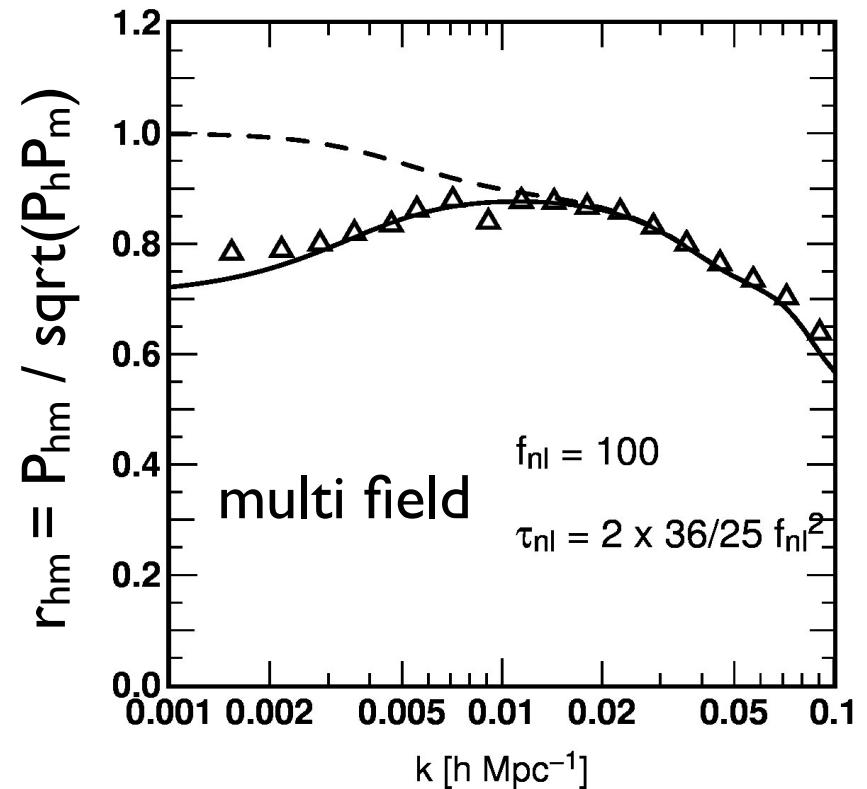
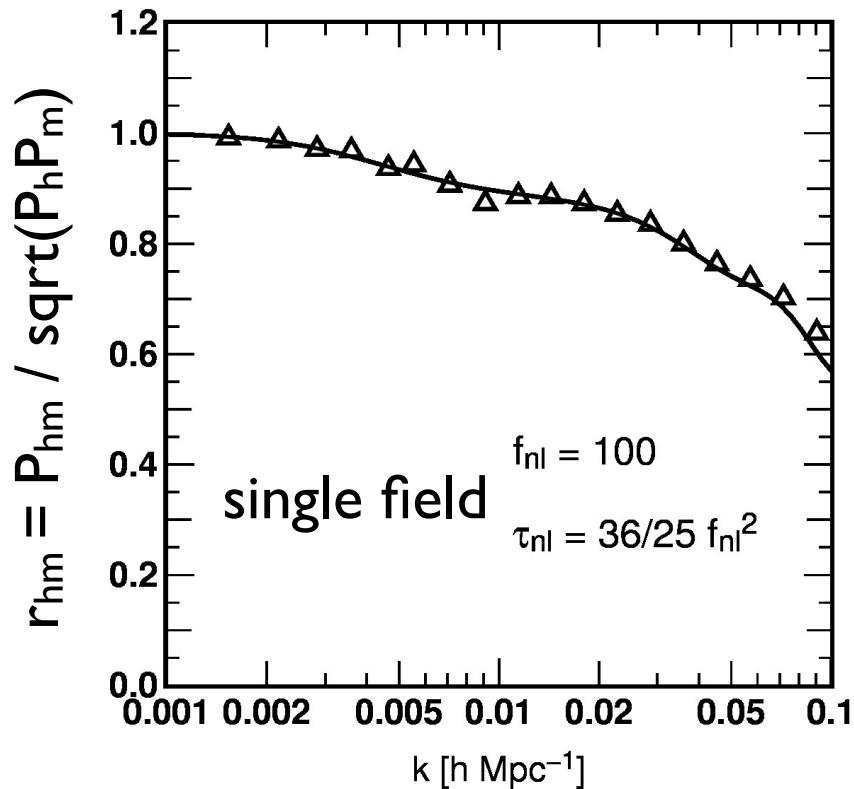


mass dependence of nG correction



See also Shandera, Dalal & Huterer '11

discussion: stochasticity btwn halo/matter



- Can we get info from the cross-correlation of galaxies and cosmic shear?

See also Tseliakhovich, Hirata & Slosar'10, Smith & LoVerde'10

Summary and future directions

We have examined the effects of multi-field local-type primordial non-Gaussianities on the halo clustering:

- $\delta_h = b_\delta \delta + b_{\chi_2} \chi_2$ is a quite general consequence
- the 2nd term yields the scale dependence in bias
- f_{nl} controls the amplitude of $P_{\delta\zeta}(k)$
- T_{nl} controls the amplitude of $P_{\zeta}(k)$
- g_{nl} gives a similar correction as f_{nl} , but it has a different mass dependence
- the nG correction becomes halo mass-dependent when 2 fields have different power spectra/transfer functions