### Kinesin Motor Mechanics: Binding, Stepping, Tracking, Gating, and Limping

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## KIAS protein winter school (High I ski resort, Jan 2011)

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## Outlines

- Basics of motors (macroscopic & microscopic engines)
- Basics of kinesin motors (structure, biochemical cycle, dynamics)
- Answering the questions addressed by S. M. Block

Macroscopic engines

### Macroscopic heat engine (Ideal engine)



$$-W \leq -W_{\max} = Q_h - Q_c$$



### Real engine (four stroke engine)





Real engine (four stroke engine)

(i) <u>intake stroke</u> performed by an isobaric expansion

(ii) <u>compression stroke</u> performed by an adiabatic compression

(iii) production of isochoric process through the "ignition of fuel", followed by an <u>power stroke</u> (adiabatic expansion)

(iv) <u>exhaust stroke</u> by an isochoric and an isobaric compression





# Microscopic engines

### Molecular Motors in the Cell









### Operational condition for molecular machines



- Size :  $\sim$  nm
- Energy scale for noncovalent bond : ~ a few kT. (Covalent bond ~ 200 kT)
- Overdamped media :

$$m\frac{dt}{dt} = -\zeta v + F \qquad v(t) = v(0)e^{-\frac{\zeta}{m}t} + \frac{1}{m}\int_{0}^{t} d\tau e^{-\frac{\zeta}{m}(t-\tau)}F(\tau) - \frac{\frac{\zeta}{m} \gg 1}{\zeta} + \frac{F(t)}{\zeta}$$

-  $f_{inertial}/f_{friction} \sim (\rho v L/\eta) = Re <<1 (\rho:density of object, v:velocity of$ object, L: size of object,  $\eta$ : viscosity of media)

Dynamics of biomolecules in the cell is dominated by Friction.

Because of different Length, Energy, and Friction scales of biomolecular dynamics in cellular environment, biological motors adopt a fundamentally different strategy from macroscopic machines to perform a work





- •Reynolds number is dimensionless
- •General properties are the same regardless of the geometry
- •Re>>1 : high Reynolds number

Intertial effect dominates, Flow becomes turbulent

•Re<<1 : low Reynolds number

Damping dominates. Flow: Laminar flow

 Flow patterns become very complex



## Life in Moving Fluids

	Re	Need to
Large whale swimming at 10 ms <sup>-1</sup>	300,000,000	by desig material
Duck flying at 20 ms <sup>-1</sup>	300,000	Increasi
Large dragonfly going 7 ms-1	30,000	moreau
Flapping wings of smallest flying insects	30	ţ
Invertebrate larva 0.3mm going at 1 mms <sup>-1</sup>	0.3	Problem Solved u cilia and anisotro
1 μm bacterium swimming at 30 μms-1	0.00003	





Problem of propulsion – Solved using cilia and flagella, i.e. anisotropic shapes and hence anisotropic drag forces.

o keep drag downgn of shape and I characteristics.

ing effect of viscosity





# Molecular motors = Enzymes

## $E + S \iff ES \longrightarrow E + P$

 $M + (ATP) \Leftrightarrow M \cdot ATP \rightarrow M \cdot ADP + P_i \rightarrow M + (ADP)$ 



ATPase activity of molecules entails "structural changes" that produce a mechanical work.

 $M_{2}$ 

Pi



Animations from Vale and Milligan (2000) Science



### Hugel et al (2002) Science 296:1103

# Kinetics of molecular motors

### **KINETICS OF MOTOR PROTEINS**

$$\frac{dP_{E_1}}{dt} = -(k_1^+ + k_3^-)P_{E_1} + k_1^- P_{E_2} + k_3^+ P_{E_3}$$
$$\frac{dP_{E_2}}{dt} = -(k_2^+ + k_1^-)P_{E_2} + k_2^- P_{E_3} + k_1^+ P_{E_1}$$
$$\frac{dP_{E_3}}{dt} = -(k_3^+ + k_2^-)P_{E_3} + k_3^- P_{E_1} + k_2^+ P_{E_2}$$
$$P_{E_1} + P_{E_2} + P_{E_3} = 1$$

$$P_{E_1}^{ss} = \frac{k_2^+ k_3^+ + k_3^+ k_1^- + k_1^- k_2^-}{\Sigma(\{k_i^\pm\})}$$

$$P_{E_2}^{ss} = \frac{k_3^+ k_1^+ + k_1^+ k_2^- + k_2^- k_3^-}{\Sigma(\{k_i^\pm\})}$$

$$P_{E_3}^{ss} = \frac{k_1^+ k_2^+ + k_2^+ k_3^- + k_3^- k_1^-}{\Sigma(\{k_i^\pm\})}$$

 $\Sigma\left(\left\{k_{i}^{\pm}\right\}\right) = k_{1}^{+}k_{2}^{+} + k_{2}^{+}k_{3}^{+} + k_{3}^{+}k_{1}^{+} + k_{1}^{-}k_{2}^{-} + k_{2}^{-}k_{3}^{-} + k_{3}^{-}k_{1}^{-} + k_{1}^{-}k_{3}^{+} + k_{1}^{+}k_{2}^{-} + k_{2}^{+}k_{3}^{-}\right)$ 

### **Steady State Solution for Reversible Cyclic Reaction**



$$P_{E_{1}}^{ss} = \frac{k_{2}^{+}k_{3}^{+} + k_{3}^{+}k_{1}^{-} + k_{1}^{-}k_{2}^{-}}{\Sigma(\{k_{i}^{\pm}\})}$$

$$P_{E_{2}}^{ss} = \frac{k_{3}^{+}k_{1}^{+} + k_{1}^{+}k_{2}^{-} + k_{2}^{-}k_{3}^{-}}{\Sigma(\{k_{i}^{\pm}\})}$$

$$P_{E_{3}}^{ss} = \frac{k_{1}^{+}k_{2}^{+} + k_{2}^{+}k_{3}^{-} + k_{3}^{-}k_{1}^{-}}{\Sigma(\{k_{i}^{\pm}\})}$$

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$$V_{3} \equiv k_{i}^{+}P_{E_{i}}^{ss} - k_{i}^{-}P_{E_{i+1}}^{ss}$$

$$= \frac{k_{i}^{+}k_{2}^{+}k_{3}^{+} - k_{i}^{-}k_{1}^{-}k_{1}^{-}k_{1}^{-}k_{1}^{-}k_{2}^{-}k_{3}^{-} + k_{1}^{-}k_{2}^{-}k_{3}^{-} + k_{2}^{-}k_{3}^{-} + k_{3}^{-}k_{1}^{-}k_{3}^{-} + k_{3}^{-}k_{1}^{-}k_{3}^{-} + k_{3}^{-}k_{1}^{-}k_{3}^{-} + k_{3}^{-}k_{1}^{-}k_{3}^{-} + k_{3}^{-}k_{1}^{-}k_{3}^{-} + k_{3}^{-}k_{3}^{-} + k$$

### **Steady State Solution for Reversible Cyclic Reaction**





### uilibrium **Nonequilibrium Steady State**

 $V_3 \equiv k_i^+ P_{E_i}^{ss} - k_i^- P_{E_{i+1}}^{ss}$  $k_1^+k_2^+k_3^+ - k_1^-k_2^-k_3^ = \frac{1}{k_1^+ k_2^+ + k_2^+ k_3^+ + k_3^+ k_1^+ + k_1^- k_2^- + k_2^- k_3^- + k_3^- k_1^- + k_3^- +$ 

$$k_{1}^{+} \rightarrow k_{1}^{+}[T]$$

$$k_{2}^{-} \rightarrow k_{2}^{-}[P]$$

$$k_{3}^{-} \rightarrow k_{3}^{-}[D]$$

$$V = \delta \frac{\prod_{i=1}^{3} k_{i}^{+}[T] - \prod_{i=1}^{3} k_{i}^{-}[D][P]}{\sum(\{k_{i}^{\pm}\})}$$

$$M_{1} \qquad M_{2}$$

$$K = \frac{j_{+}}{j_{-}} = \frac{k_{1}^{+} k_{2}^{+} k_{3}^{+}[T]}{k_{1}^{-} k_{2}^{-} k_{3}^{-}[D][P]}$$

$$1 = \frac{k_{1}^{+} k_{2}^{+} k_{3}^{+}[T]_{eq}}{k_{1}^{-} k_{2}^{-} k_{3}^{-}[D]_{eq}[P]_{eq}}$$

$$M_{1} \qquad M_{2}$$

$$M_{2} \qquad M_{3}$$

$$\rightarrow k_{1}^{+}[T]$$

$$\rightarrow k_{2}^{-}[P]$$

$$\rightarrow k_{3}^{-}[D]$$

$$V = \delta \frac{\prod_{i=1}^{3} k_{i}^{+}[T] - \prod_{i=1}^{3} k_{i}^{-}[D][P]}{\sum \left(\left\{k_{i}^{\pm}\right\}\right)}$$

$$ATP$$

$$M_{1}$$

$$M_{2}$$

$$M_{1}$$

$$M_{2}$$

$$M_{1}$$

$$M_{2}$$

$$M_{2}$$

$$M_{1}$$

$$M_{2}$$

$$M_{2}$$

$$M_{2}$$

$$M_{2}$$

$$M_{2}$$

$$M_{2}$$

$$M_{3}$$

 $\Delta$  $( L^{-J} ) / ( L^{-J} eq ) )$ 

$$E_{1} \stackrel{k_{1}}{\underset{k_{3}}{\overset{k_{2}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k_{3}}{\underset{k_{3}}{\overset{k_{3}}{\underset{k}$$

$$k_1^-k_3^+ + k_1^+k_2^- + k_2^+k_3^-$$

Under ex  

$$V = \delta \frac{\prod_{i=1}^{N}}{\sum(\{k_i^{\pm}\})}$$

$$= \delta \frac{k_T^+[T]k_S^+k_{hyd}^+k_{-p}^+k_{-D}^- - k_T^-k_S^-k_{hyd}^-k_{-p}^-[P]k_{-D}^-[D]}{\sum(\{k_i^{\pm}\})}$$

$$k_i^{\pm} \rightarrow k_i^{\pm} \exp(\pm f\delta_i^{\pm}/k_B T) \qquad j_+ \qquad j_-$$

$$V(f) = \delta \frac{\left(\prod_{i=1}^{N}k_i^+[T]\right)e^{-f\sum_i \delta_i^+/k_B T}}{\sum(f)} \qquad \left(\prod_{i=1}^{N}k_i^-[D][P]\right)e^{f\sum_i \delta_i^-/k_B T}}{\sum(f)}$$

$$E_i \delta_i^+ + \sum_i \delta_i^- = \delta = 8 \text{ nm}$$

$$K = j_+/j_- = K^o e^{-f\delta/k_B T} = \left(K_{eq} \frac{[T]}{[D][P]}\right)e^{-f\delta/k_B T}$$

Kinesins

# Transport motors in cellular systems

- Transport motors (kinesin, myosin, dynesin) carry cellular material along the complex network of cytoskeletal filaments such as microtubules and actin.
- Molecular motors catalyze the hydrolysis of ATP so as to proceed along cytoskeletal filament.
- Kinesin's speed (Rapid transport of organelle along the axon is accomplished by directed motions of kinesin)
  - V ~ 1 $\mu$ m/sec  $\Rightarrow$  To travel 1 m  $\Rightarrow$  t ~ 11 days.
  - cf. D ~ 10  $\mu$ m<sup>2</sup>/sec  $\Rightarrow$  To travel 1m  $\Rightarrow$  t > 300 years





axon of giant squid

# Microtubules

- consist of multiple alpha and beta-tubulin dimers.
- In vivo : 13 protofilament, straight along the axis
- In vitro : 11-15 protofilament, helical along the axis.
- Each dimer is highly charged (net charge = -34 e)





# **Crystal structure of kinesin-1**

### coiled-coil association



### nucleotide (ATP, ADP.Pi, ADP) binding site















• 45 kinesin genes



- Single-headed kinesin (KIF1A)
- (-) end-directed kinesin (NCD).

- 45 kinesin genes
- kinesin-1 : Conventional kinesin, responsible for material transport. (the most well studied kinesin)
- kinesin-5 (Eg5) : kinesin tetramer responsible for bipolar spindle formation leading to the cell division.
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head. head B head A head B



Understanding biochemical cycle (Microscopic rates and binding constant of kinesin)

## NECK LINKER DOCKING MODEL

Q: Is the head-neck linker docking model correct (and does it suffice to explain actual stepping)? Does kinesin undertake a conformational "power stroke", or something like it (and if so, how large is it)?



Figure 2 Electron paramagnetic resonance spectra for kinesin C333–MSL in several nucleotide states, both free in solution and bound to microtubules. The two sets of resonance peaks are indicated by arrows. The narrower resonance peaks are indicative of a highly mobile probe, whereas the wider set of resonance peaks (highlighted by the vertical dashed lines) are indicative of restricted mobility and emerge in the triphosphate states on microtubules. This mobility shift can be modelled by a restriction in probe motion from a cone angle of  $\sim 120^{\circ}$  to  $32^{\circ}$  (ref. 50).




#### Table 1 FRET between donor (coumarin, CPM) and acceptor (tetramethylrhodamine, TMR) probes attached to the neck linker (C333) and the catalytic core (C220) in wild-type kinesin monomer and two ATP nonhydrolysing mutants

Kinesin (K349–C220, C333)	Nucleotide	MT	Energy transfer (%)
Wild type	ADP	_	87.6 ± 3.3
	AMP-PNP	_	$84.4 \pm 0.2$
	Nucleotide-free	+	76.4 ± 2.8
	AMP-PNP	+	93.4 ± 1.3



333 nucleotide-free

333 AMP-PNP

333 ADP-AIF4 -

333 ADP

K349 AMP-PNP K349 nucleotide-free







Ma & Taylor JBC (1997) 272:724-730

$$M + ATP \underset{k_{-1}}{\overset{k_1}{\longrightarrow}} M \cdot ATP \overset{k_{hyd}}{\longrightarrow} M \cdot (ADP \cdot P_i) -$$

$$k = \frac{k_{cat}[ATP]}{K_{M} + [ATP]} = \frac{k_{cat}[ATP]}{\frac{k_{1} + k_{cat}}{k_{-1}} + [ATP]}$$

$$\star ATP b$$

$$\star Pi rele$$

$$\star ATP p$$

$$\star ADP r$$

$$\star Cat = 0$$



$$k_{cat}^{-1} = k_{hyd}^{-1} + k_{dPi}^{-1} + k_{dADP}^{-1}$$

binding kinetics, thermodynamics elease kinetics

promoted dissociation of MT-kinesin complex

P release kinetics w or w/o MT

#### Dimeric Kinesin



	$(\mu M^{-1} s^{-1})$	$(s^{-1})$	(s <sup>-1</sup> )
K401	2	71	300
K341	20	200	300

<sup>a</sup> The scheme depicts the steps in the ATPase pathway for monomeric and dimeric kinesin with rate constants defined in the table. For dimeric kinesin, one turnover of ATP requires one and one-half turns of the ATPase cycle shown. <sup>b</sup> Maximum steady-state rate of ATP hydrolysis per enzyme active site.

#### Monomeric Kinesin

	Rate constant
$ak_T^+(\equiv k_T)$	$k_T^{\rm o} = 2.0 \pm 0.8 \ \mu {\rm M}^{-1} {\rm s}^{-1.5}$
${}^{b}k_{T}^{-}(\equiv k_{-T})$	$k_{-T} = 71 \pm 9 \text{ s}^{-1.5}$
$k_{S}^{+}(\equiv k_{S})$	$k_S \gtrsim (100 \ \mu s)^{-1}$
$^{d}k_{S}^{-}(\equiv k_{-S})$	
$k^{e}k^{+}_{-D}(\equiv k_{-D})$	$k_{-D[L]} = 75 - 100 \text{ s}^{-1.7}$
	$k_{-D[T]} = 1 \text{ s}^{-1.7}$
$f_{k_{-D}}(\equiv k_D)$	No data
${}^{g}k_{h}^{+}(\equiv k_{h})$	$k_h > 100 \pm 30 \text{ s}^{-1.3}$
${}^{h}k_{h}^{-}(\equiv k_{-h})$	$k_{-h} = 1.3  \mathrm{s}^{-1}$
$^{i}k_{-P}^{+}(\equiv k_{-P})$	$k_{-P} = 50 \text{ s}^{-1}$
$^{j}k_{-P}^{-}(\equiv k_{P})$	No data
$k_{k_{h,-P}}$	$k_{h,-P} = 100-300 \text{ s}^{-1}$
	$k_{-h,P} = 34 \text{ M}^{-1} \text{ s}^{-1/2}$

 Table 2
 Rate and equilibrium constants for the microscopic steps along the cycle

<sup>a</sup> Bi-molecular rate constant for ATP binding to the nucleotide free kinesin head. <sup>b</sup> Rate constant for ATP dissociation from the ATP bound kinesin head. <sup>c</sup> Rate constant for kinesin stepping. <sup>d</sup> Rate constant for kinesin backstepping. <sup>e</sup> Rate constant for ADP dissociation. <sup>f</sup> Rate constant for ADP re-binding. <sup>g</sup> Rate constant for hydrolysis at the catalytic site. The free energy change for ATP hydrolysis ATP  $\Rightarrow$  ADP + P<sub>i</sub> under standard aqueous conditions (aq., 1 atm, 25 °C) is  $\Delta \mu^{\circ} = -12 k_B T$ . <sup>h</sup> Rate constant for ATP synthesis. <sup>i</sup> Rate constant for phosphate dissociation. <sup>j</sup> Rate constant for phosphate re-binding. <sup>k</sup> Rate constant for hydrolysis followed by phosphate release.



#### Equilibrium constant

 $K_T = k_T^{\rm o}/k_{-T} = (35 \ \mu {\rm M})^{-1.5}$ 

No data

$$K_{D[L]} = k_D^{o}/k_{-D} = 5 \times 10^4 \text{ M}^{-1.7}$$
  
 $K_{D[T]} = k_D^{o}/k_{-D} = 5 \times 10^6 \text{ M}^{-1.7}$ 

 $K_h < 39$ 

No data

$$K_{h,-P} = 200 \text{ s}^{-1}/34 \text{ M}^{-1} \text{ s}^{-1} = 6 \text{ M}^{-2}$$

	MT	Neck-linker
К.Ф	Strongly bound	Disordered (unzippered)
K.ATP	Strongly bound	Ordered (zippered)
K.ADP/Pi	Strongly bound	Ordered (zippered)
K.ADP	Weakly bound	Disordered (unzippered)



Cryo-EM



Rice et al (1999) Nature

#### From a number of ensemble and single molecule experiments....

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Rice et al (1999) Nature



#### From a number of ensemble and single molecule experiments....







# hydrolysis





AMPPNP

ADP



# An atomic-level mechanism for activation of the kinesin molecular motors

#### Charles V. Sindelar<sup>12</sup> and Kenneth H. Downing

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В





PNAS | March 2, 2010 | vol. 107 | no. 9 | 4111–4116



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Monitor the response of kinesin motors under ATP concentration and/or force perturbation

### Motor Velocity



### Run Length

# Questions from Biophys. J. (2007) 92: 2986-2995

- Does kinesin take substeps? If so, over what time and distnace scales?
- What's the kinesin walking pattern, and what do we learn about its mechanics from this? (sym. HoH, asym HoH, inchworm)
- How do the two kinesin heads mange to stay out of phase with one another during the stepping cycle (i.e., how are they "gated")?
- Where in the kinesin biochemical pathway is forward motion produced?
- Is the bacstepping cycle a reversal of the forward cycle, and does kinesin generate ATP under super-stall loads that force it to move backward?

# Questions from Biophys. J. (2007) 92: 2986-2995

- Conversely, when kinesin is sped up by an assisting force, is it going through its normal biochemical cycle or by some other pathway ?
- When stepping processively, does kinesin spend most of its time in a two-heads bound (2HB) state or a one-head bound (1HB) state?
- Is the head-neck linker docking model correct (and does it suffice to explain actual stepping)? Does kinesin undertake a conformational "power stroke", or something like it (and if so, how large is it)?
- How does kinesin manage to track parallel to a single protofilament of the microtubule?

## Q:Where in the kinesin biochemical pathway is forward motion produced?



•Release of stored strain upon unbinding of the trailing head empowers an 8-nm advance of the entire molecules (Hancock & Howard)

•ATP binding induces the docking of the neck-linker on the leading head to produce motion of the partner head (Rice et al)





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## Q:What's the kinesin walking pattern, and what do we learn about its mechanics from this? (symmetric hand-over-hand, asymmetric hand-over-hand, inchworm)







### FIONA

#### Yildiz, Tomishige, Vale, Selvin Science (2004) 303: 676







Yildiz, Tomishige, Vale, Selvin Science (2004) 303: 676

Dwell time distribution for the step of a single kinesin head : two poissonian steps with rate k

$$s \xrightarrow{k} p \xrightarrow{k} s \xrightarrow{k} \rightarrow s$$

$$P(t) = \int_{0}^{t} d\tau P_{1}(\tau) P_{2}(t - \tau)$$

$$= \int_{0}^{t} d\tau k_{1} e^{-k_{1}\tau} k_{2} e^{-k_{2}(t - \tau)}$$

 $\lim_{k_1,k_2\to k} P(t) = k^2 t e^{-kt}$ 

# Symmetric HoH or Asymmetric HoH ?



Asbury et al. Science (2003) 302:2130

### Symmetric HoH or Asymmetric HoH ?





The longer the coiled-coil stalk, the less the kinesins limp

Asbury et al. Science (2003) 302:2130









Block and coworkers PNAS (2009) 106:17007

Q: How do the two kinesin heads manage to stay out of phase with one another during the stepping cycle (i.e., how are they "gated")?

"Gated rear head" mechanism: strain increases the detachment rate of the rear head from the MT.

"Gated front head" mechanism: ATP binding to the leading head is suppressed through internal strain.

Guydosh & Block PNAS (2006) 103:8054





Addition of ADP·BeF<sub>x</sub> or AMP·PNP (ATP analog that strongly binds catalytic site) to kinesin causes extended dwell. Kinesin is rescued from this extended dwell only after a backstep  $\rightarrow$ ATP analog dissociates when it is in the front head

Guydosh & Block PNAS (2006) 103:8054





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Uemura & Ishiwata Nature Struct. Biol. (2003) 10:308

### Q: Does kinesin take substeps? If so, over what time and distance scales?







#### Coppin et al. PNAS (1996) 93:1913



#### Yanagida and coworkers Nature Cell Biol. (2000) 3:425



### Carter & Cross Nature (2005)

Q: When stepping processively, does kinesin spend most of its time in a two-heads bound (2HB) state or a onehead bound (IHB) state?

What is the nature of weakly-bound ADP state?












Mori, Vale, Tomishige Nature (2007) 450: 750













Mori, Vale, Tomishige Nature (2007) 450: 750



8 nm centre-of-mass step

Mori, Vale, Tomishige Nature (2007) 450: 750



wt: wild type BSR : label L12 : mutant (MT binding reduced)

### Fluorescence polarization microscope (FPM)

















# Q: Does kinesin move by a power stroke or by a Brownian ratchet mechanism



## Athermal fluctuation can induce a unidirectional transport in spatially asymmetric potential



FIG. 1. Model potential is infinite at either end of, and below, ramp. Gravitational field and random force with friction  $\zeta$  exist above ramp.

### A.L.R. Bug and B.J. Berne (1987) PRL 59, 948

$$= (4\pi Dt)^{-1} \exp(-\{(x-x_0)^2 + [z-Z+(mg/\zeta)t]^2\}/4Dt),$$

$$\left[\frac{d\Delta z_i}{dT}\right]^{1/2} \frac{h_0}{l_0} \int_0^\infty \exp\left[-\left(\frac{mg\Delta z_i}{kT}\right)^{1/2} \frac{h_0}{l_0}y\right] \operatorname{erfe}(y) dy.$$

$$k_{i-1}p_{i-1} - k_ip_i, \quad 1 < i < N;$$
  
 $k_1 - k_1p_1; \quad dp_N/dt = k_{N-1}p_{N-2}$ 

the uphill rate constant  $k_i \equiv f_i/\tau$ .



Kolomeisky & Fisher, Annu. Rev. Phys. Chem. (2007)





# Q: Is the bacstepping cycle a reversal of the forward cycle, and does kinesin generate ATP under super-stall loads that force it to move backward?





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$$\frac{k_0 - x_{TS} / k_B T}{k_S - x_{-1} / k_B T} = \frac{k_f^o}{k_b^o} \exp\left[-f \times \frac{(x_0 - x_{-1})}{k_B T}\right]$$



$$\sum_i \delta_i^+ + \sum_i \delta_i^- = \delta = 8 \ \mathrm{nm}$$

$$p\left(-f\delta/k_{B}T\right) = \left(K_{eq}\frac{[T]}{[D][P]}\right)\exp\left(-f\delta/k_{B}T\right)$$

### Multi-cycle model accounts for the backstep dynamics of kinesin motors Hyeon, Klumpp & Onuchic (2009) Phys. Chem. Chem. Phys. 11:4899



$$K_{\mathcal{F}^+ \oplus \mathcal{B}_T^+}(f) = \underbrace{j_+}_{j_-} = \frac{k_S^+}{k_{\mathcal{B}_T^+}^{eff}} \exp\left(-\frac{f(\delta_{\mathcal{F}^+} + \delta_{\mathcal{B}_T^+})}{k_B T}\right).$$

 $f_{stall} = k_B T / (\delta_{\mathcal{F}^+} + \delta_{\mathcal{B}_T^+}) \times \log\left(k_S^+ / k_{\mathcal{B}_T^+}^{eff}\right)$ 

### Q: Conversely, when kinesin is sped up by an assisting force, is it going through its normal biochemical cycle or by some other pathway ? KSTLLFGQRAKTIKNTVSVNVELTAEQWKKK. 500 msec no nucleotide



- Neck-Linker Generated Strain Α
- weakly bound (D ADP + ck-linker docking 16 nm head movement
- **Externally Generated Strain** в





-16 nm head movement

16 nm head movement





Vale & coworkers, *Cell* (2008) Vol 134, 1030-1041

## **KINETICS OF MOTOR PROTEINS**

$$\frac{dP_{E_1}}{dt} = -(k_1^+ + k_3^-)P_{E_1} + k_1^- P_{E_2} + k_3^+ P_{E_3}$$
$$\frac{dP_{E_2}}{dt} = -(k_2^+ + k_1^-)P_{E_2} + k_2^- P_{E_3} + k_1^+ P_{E_1}$$
$$\frac{dP_{E_3}}{dt} = -(k_3^+ + k_2^-)P_{E_3} + k_3^- P_{E_1} + k_2^+ P_{E_2}$$
$$P_{E_1} + P_{E_2} + P_{E_3} = 1$$

$$V_{3} \equiv k_{i}^{+} P_{E_{i}}^{ss} - k_{i}^{-} P_{E_{i+1}}^{ss} \qquad j_{+} \qquad j_{-}$$

$$= \frac{k_{1}^{+} k_{2}^{+} k_{3}^{+}}{k_{1}^{+} k_{2}^{+} + k_{3}^{+} k_{1}^{+} + k_{1}^{-} k_{2}^{-} k_{3}^{-}} \qquad k_{1}^{-} k_{2}^{-} k_{3}^{-} \qquad k_{1}^{-} k_{2}^{-} k_{3}^{-} + k_{1}^{-} k_{3}^{-} + k_{1}^{+} k_{2}^{-} + k_{2}^{+} k_{3}^{-}} \qquad j_{+} = 0 \Rightarrow \qquad \textbf{Equilibrium}$$

$$j \neq 0 \Rightarrow \qquad \textbf{Nonequilibrium Steady}$$

$$k_{1}^{+} \rightarrow k_{T}^{+}[T] \qquad j \neq 0 \Rightarrow \qquad \textbf{Nonequilibrium Steady}$$

$$k_{2}^{-} \rightarrow k_{-P}^{-}[P] \qquad V = \delta \frac{\prod_{i=1}^{3} k_{i}^{+}[T] - \prod_{i=1}^{3} k_{i}^{-}[D][P]}{\sum(\{k_{i}^{\pm}\})} \qquad K = \frac{j_{+}}{j_{-}} = \frac{k_{1}^{-}}{k_{1}^{-}}$$

## in the presence of backward load

## **Steady State Solution for Reversible Cyclic Reaction**



## State

 $k_1^+ k_2^+ k_3^+ [T]$  $k_{2}^{-}k_{3}^{-}[D][P]$  $k_i^+ \rightarrow k_i^+ \exp\left(-f\delta_i / k_B T\right)$  $k_i^+ \rightarrow k_i^- \exp(+f\delta_i / k_B T)$ 

# Q: How does kinesin manage to track parallel to a single protofilament of the MT?



MP Sheetz and coworkers Biophys. J. (1995) 69:2011-2023



### Block et al. PNAS (2003) 100:2351--2356









# Questions from Biophys. J. (2007) 92: 2986-2995

- Does kinesin take substeps? If so, over what time and distnace scales?
- What's the kinesin walking pattern, and what do we learn about its mechanics from this? (sym HoH, asym HoH, inchworm)
- How do the two kinesin heads mange to stay out of phase with one another during the stepping cycle (i.e., how are they "gated")?
- Where in the kinesin biochemical pathway is forward motion produced?
- Is the bacstepping cycle a reversal of the forward cycle, and does kinesin generate ATP under super-stall loads that force it to move backward?

# Questions from Biophys. J. (2007) 92: 2986-2995

- Conversely, when kinesin is sped up by an assisting force, is it going through its normal biochemical cycle or by some other pathway?
- When stepping processively, does kinesin spend most of its time in a two-heads bound (2HB) state or a one-head bound (1HB) state?
- Is the head-neck linker docking model correct (and does it suffice) to explain actual stepping)? Does kinesin undertake a conformational "power stroke", or something like it (and if so, how large is it)?
- How does kinesin manage to track parallel to a single protofilament of the microtubule?