

# Theory of dispersion forces and its application to molecular assemblies on a crystalline surface

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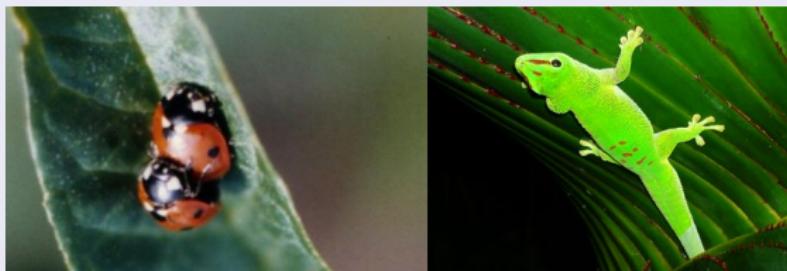
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# Outline

- 1 Introduction
- 2 van der Waals Forces
  - Lifshitz theory of dispersion forces
- 3 Template-directed molecular self-assembly
  - Anisotropic van der Waals forces
  - van der Waals forces on a metallic substrate
  - Ionic screening and sound velocities
  - Phonon-induced anisotropy in van der Waals forces

# vdW forces for pedestrians

How does the van der Waals force work?



- pairwise summation method
- Casimir force
- fluctuation-dissipation theorem

V. A. Parsegian, *van der Waals Forces* (2006)

# van der Waals forces everywhere

- bio-physics, chemistry: interfacial and cohesion energies
- soft-condensed matter physics: physical adsorption
- nano-science: molecular modeling; graphite binding

## Theoretical Approach

- ① density-functional theory; tight-binding method; RPA.
- ② Lifshitz's theory of dispersion forces.
- ③ polymer dynamics (Brownian motion).

# van der Waals forces everywhere

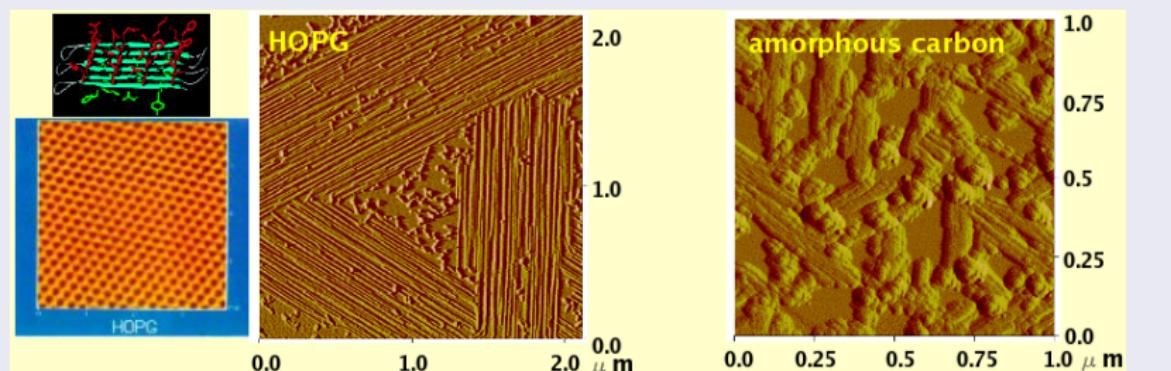
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# Oriented-patterned formation

## Template-directed molecular self-assemblies



*Phys. Rev. Lett.* **96**, 18301 (2006)

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## 2 van der Waals Forces

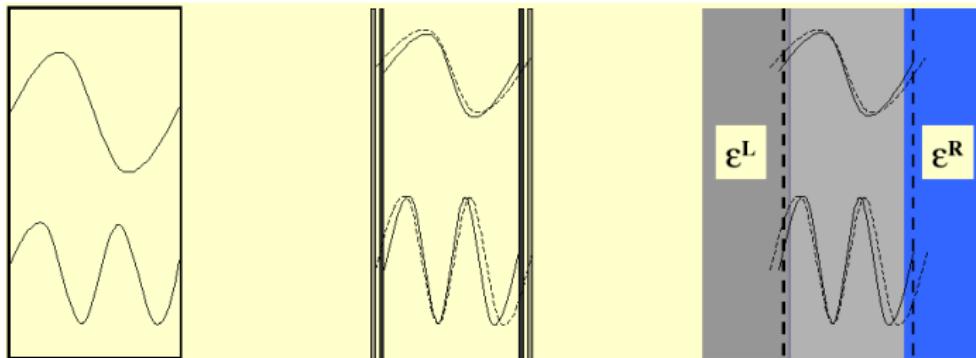
- Lifshitz theory of dispersion forces

## 3 Template-directed molecular self-assembly

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# Lifshitz theory

From Planck, Casimir, to Lifshitz.

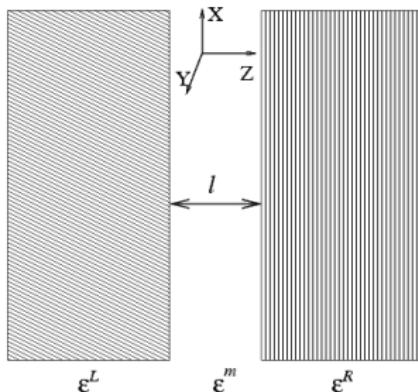


- Hamaker coefficient  $A_H$ :

$$E = -\frac{A_H}{12\pi\ell^2}$$

# Calculation of free energy between two slabs

- for mode  $\omega_j$ ,  $F_j = -k_B T \ln Z_j$ ;  $Z_j = \sum_n \exp \left[ -(n + \frac{1}{2}) \frac{\hbar \omega_j}{k_B T} \right]$

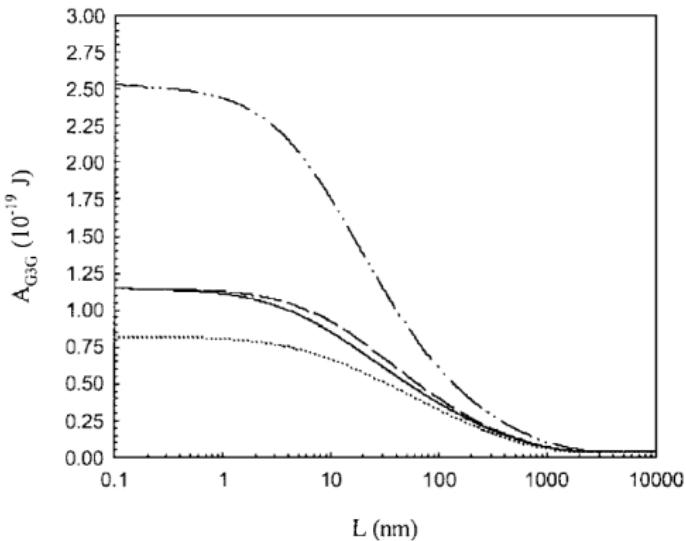


- solve  $\nabla \cdot \vec{D} = ik_x D_x + ik_y D_y + \frac{\partial D_z}{\partial z} = 0$ ;  $\vec{D} = \epsilon \vec{E}$

$$A_H = -\frac{3\ell^2 k_B T}{\pi} \sum_{\omega_j, \vec{k}} \ln \left[ 1 - \left( \frac{\epsilon_L(\omega, \vec{k}) - 1}{\epsilon_m(\omega, \vec{k}) + 1} \right) \left( \frac{\epsilon_R(\omega, \vec{k}) - 1}{\epsilon_m(\omega, \vec{k}) + 1} \right) e^{-2k\ell} \right]$$

# Hamaker coefficient between two graphite slabs

Hamaker coefficient is constant within non-retarded regime.



Dagastine *et al.*, J. Colloid Interface Sci. 249, 78 (2002)

# Spatial dispersions in the dielectric function

## Bringing spatial dispersions to the theory of vdW forces $\epsilon(\omega, \vec{k})$

- $\mathbf{D}(\omega, \vec{r}) = \int \epsilon(\omega, \vec{r}, \vec{r}') \mathbf{E}(\omega, \vec{r}') d\vec{r}'$
- Characteristic length dictates if  $k$  can be taken as  $k \approx 0$ .

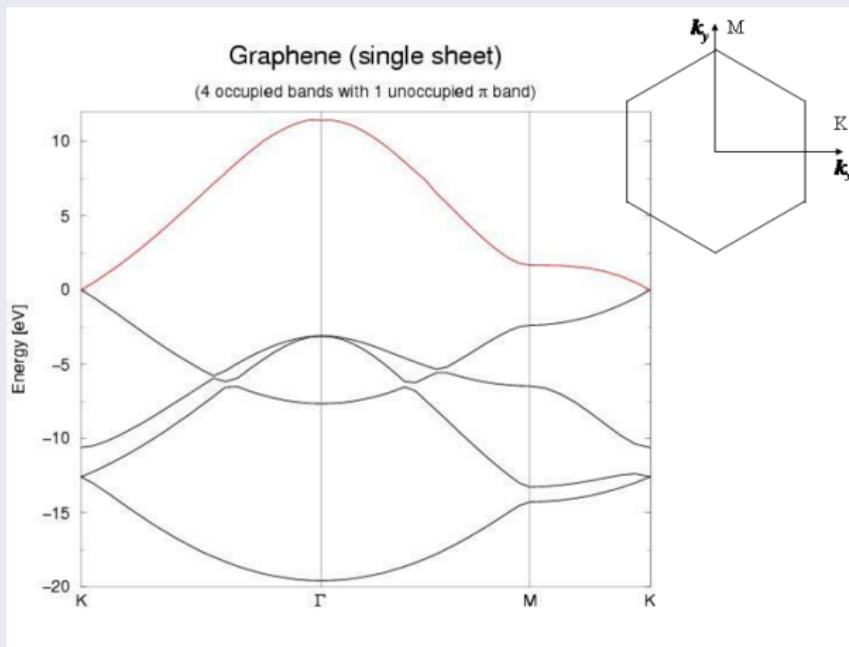
## Bringing spatial dispersions to the theory of vdW forces

- at larger (finite) wavevectors  $\vec{k}$ , the screening is not as effective as at  $\vec{k} \rightarrow 0$ .
- non-retarded Hamaker constant is separation dependent.

*Phys. Rev. B* **71**, 235412 (2005).

# Numerical example: graphite

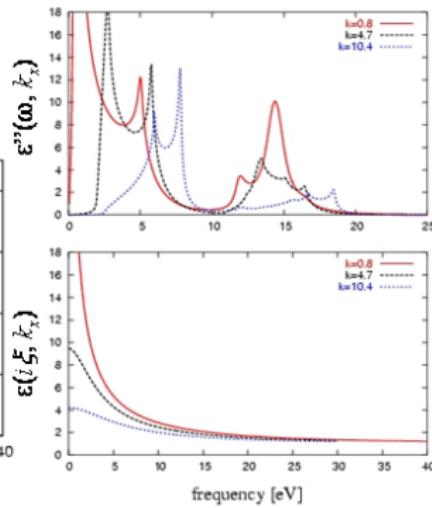
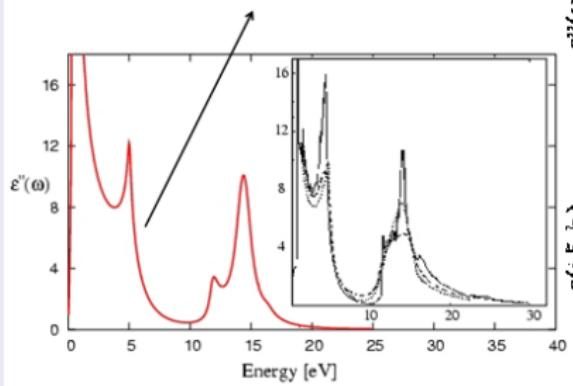
## Band structure



# Dielectric screening of graphite

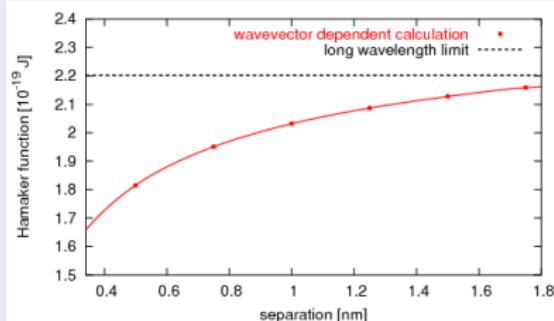
Dielectric function  $\epsilon(\omega, \vec{k})$

dielectric function  $\epsilon(\omega, \vec{k})$   
computed within the RPA:



# Hamaker coefficient between two graphite slabs

Hamaker coefficient depends on separations



Hamaker coefficient [ $A_H$  in the unit of  $10^{-19} \text{ J}$ ;  $\ell$  in the unit of nm]

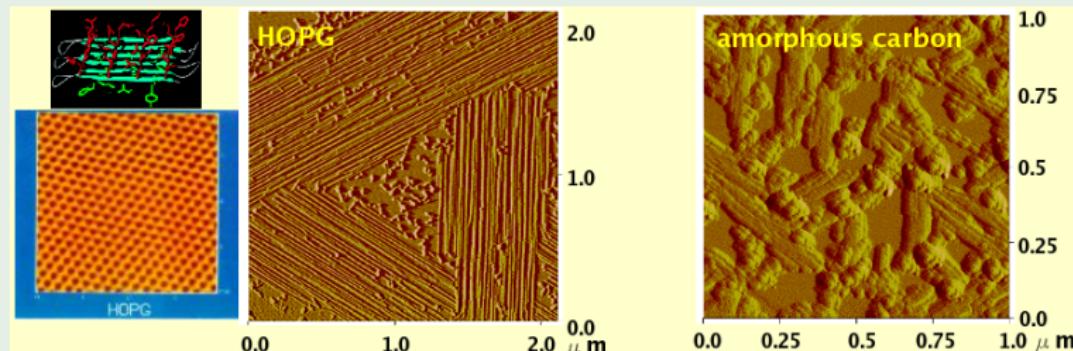
|                         | $\ell = 0.5$ | $\ell = 1.0$ | $\ell \gg 1$ | Expt <sup>†</sup> |
|-------------------------|--------------|--------------|--------------|-------------------|
| graphite-water-graphite | 0.72         | 0.87         | 0.99         | 0.5-1.0           |
| graphite-air-graphite   | 1.82         | 2.03         | 2.20         | 2.1-5.9           |

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# Patterned adsorption on graphite

## Example

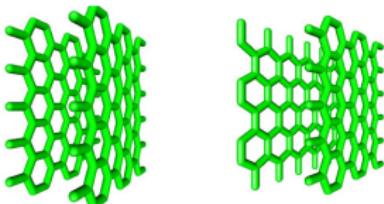


protein fibrils; micelles.

# Anisotropy induced by $\epsilon(\omega, \vec{k})$

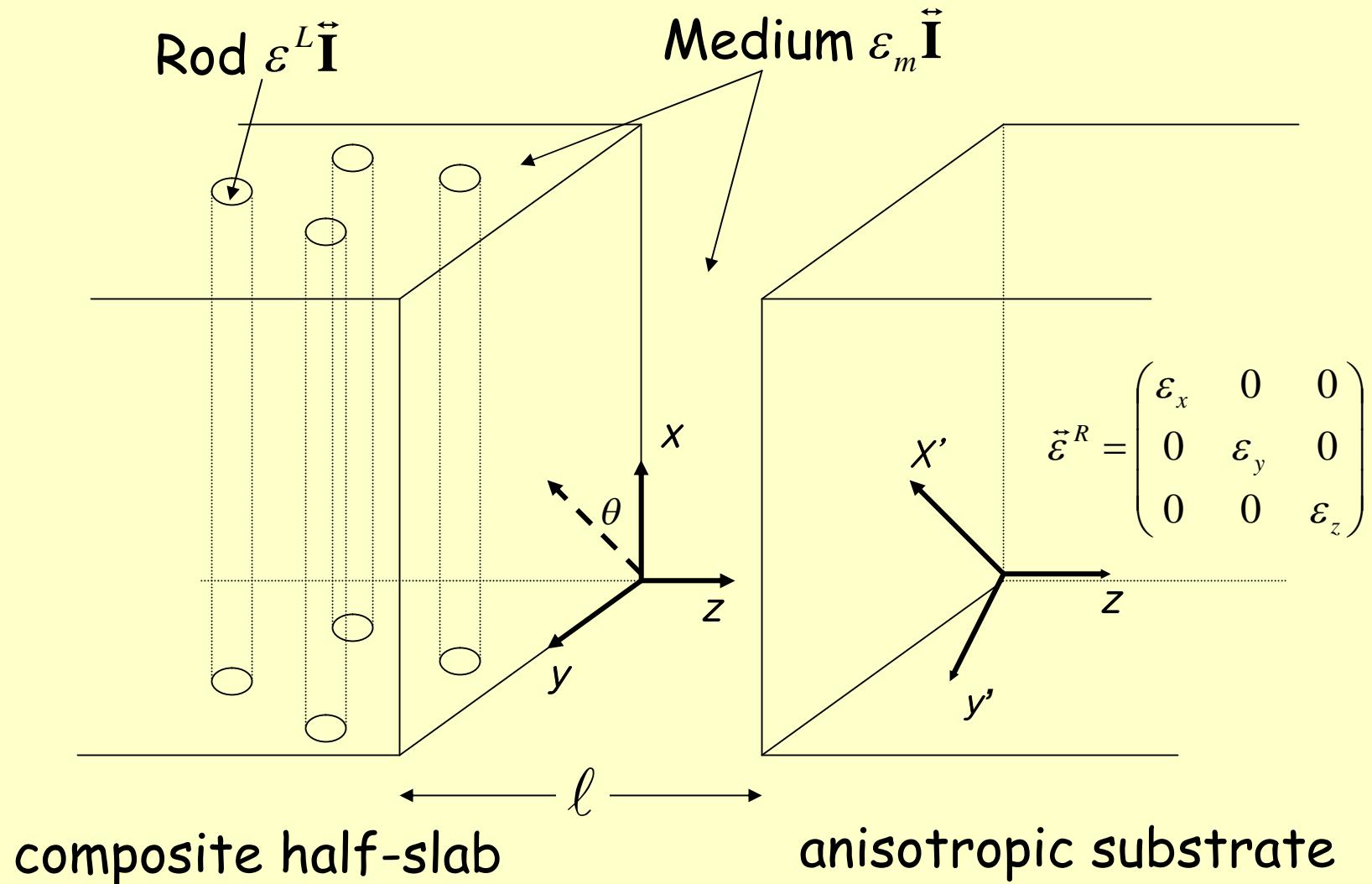
Anisotropic screening due to the directionality of  $\vec{k}$

- $\epsilon(\omega) \rightarrow \begin{pmatrix} \epsilon(\omega, k_x) & 0 & 0 \\ 0 & \epsilon(\omega, k_y) & 0 \\ 0 & 0 & \epsilon(\omega, k_z) \end{pmatrix}$



→ compute van der Waals binding energies for different orientations.

# anisotropic vdW interaction



# Analysis of the orientational ordering

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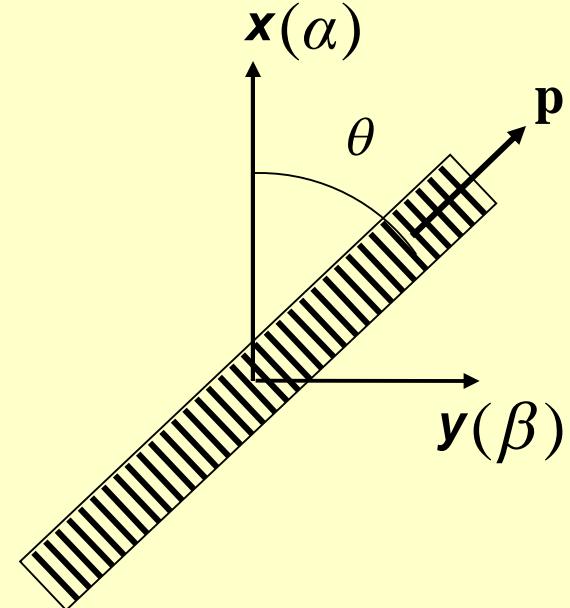
## Smoluchowski equation

$$\frac{\partial \psi}{\partial t} = D_{rot} \left( \mathbf{p} \times \frac{\partial}{\partial \mathbf{p}} \right) \cdot \left[ \mathbf{p} \times \frac{\partial \psi}{\partial \mathbf{p}} + \frac{\psi}{kT} \mathbf{p} \times \frac{\partial U}{\partial \mathbf{p}} \right]$$

↓  
steady-state solution

$$\frac{\partial \ln \psi}{\partial p_x} = - \frac{1}{kT} \frac{\partial U}{\partial p_x}$$

↓  
probability density function

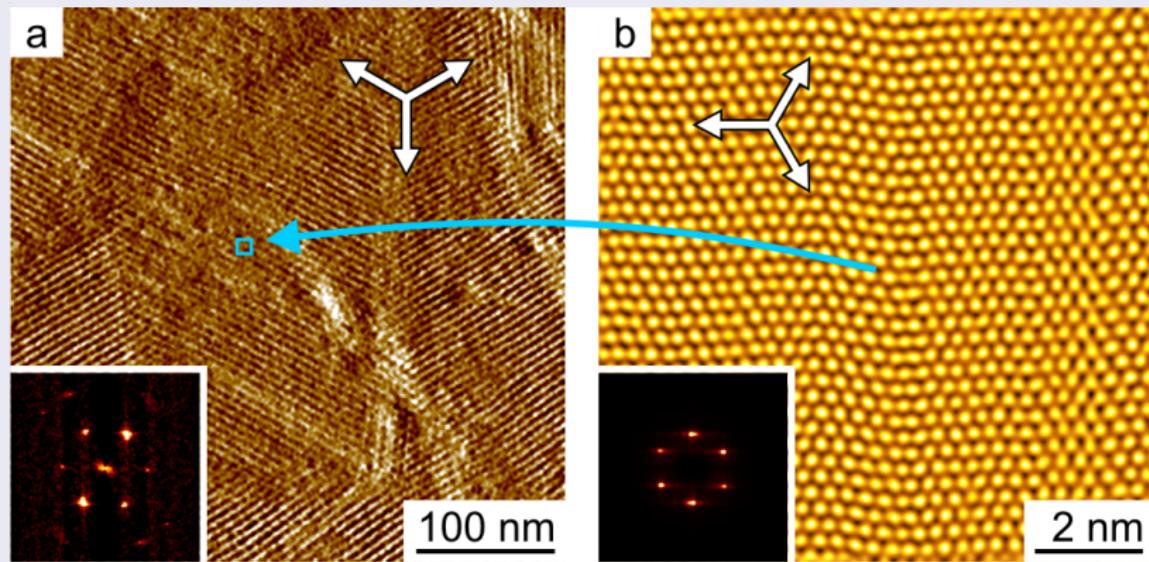


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# Adsorption of micelles on a gold (111) surface

## Template-directed molecular self-assembly on a gold (111) surface



# Puzzle: patterned physisorption on a metallic substrate

Why these do not work

image method

epitaxial principle

pairwise summation theory

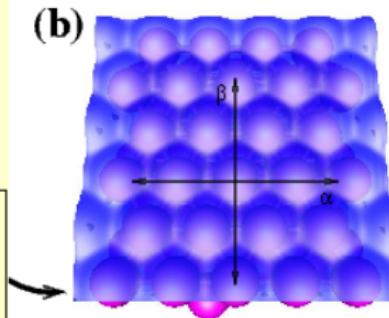
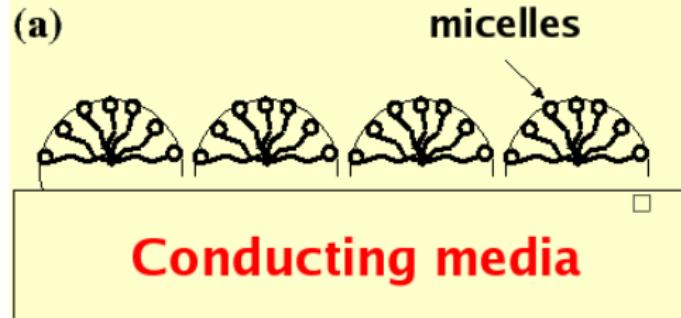
anisotropic vdW force

delocalized conduction electrons

isotropic electronic screening:

$$\epsilon(\omega \rightarrow 0) \longrightarrow \infty.$$

Figure: (a) Micelles on a conducting substrate. (b) A gold (111) surface.



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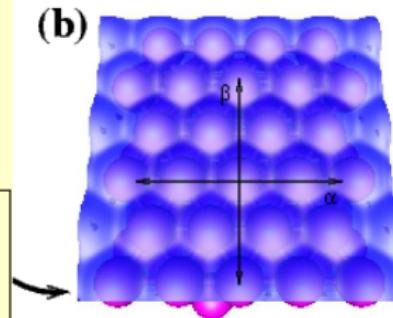
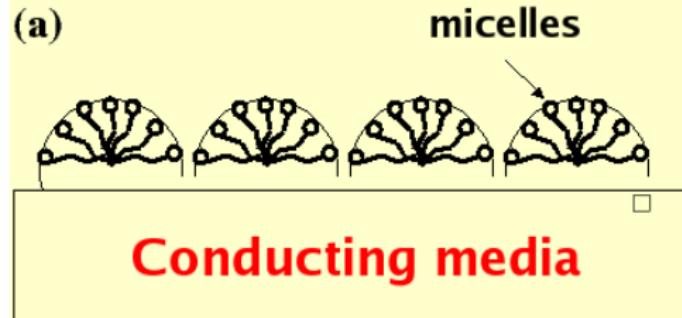
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# Dressed phonon in metals

Screening in metals:  
charge redistribution

electronic screening  
(plasma model)

$$\epsilon^{el}(\omega) = 1 - \frac{4\pi Ne^2/m}{\omega^2}$$

dressed phonon screening

$$\frac{1}{\epsilon(\omega, \vec{k})} = \frac{1}{\epsilon^{el}(\omega)} \frac{1}{\epsilon_{dressed}^{ion}(\omega, \vec{k})}$$

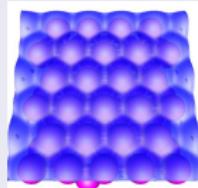
$$\begin{aligned}\epsilon_{dressed}^{ion}(\omega, \vec{k}) &= 1 - \tilde{\omega}^2(\vec{k})/\omega^2 \\ \tilde{\omega}(\vec{k}) &= c_s(\hat{k})k\end{aligned}$$

Ashcroft and Mermin, *Solid State Physics* (1976).

# Sound velocity is anisotropic in metals

Within continuum mechanics,

$$\begin{aligned}c_s^2(\hat{k}) &= \left( \frac{\partial p}{\partial \rho} \right)_V \\&= \left( \frac{\partial p^{el}}{\partial \rho} \right)_V + \left( \frac{\partial p^{ion}}{\partial \rho} \right)_V\end{aligned}$$

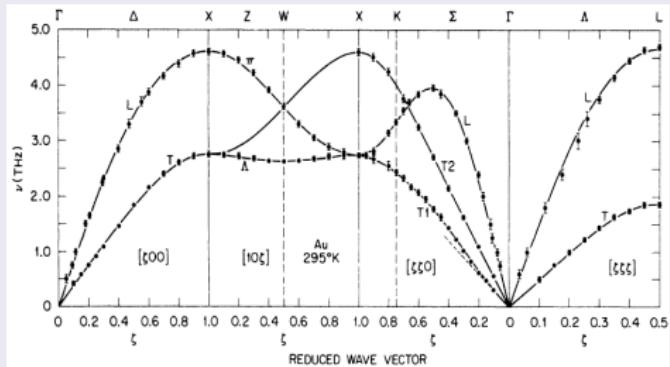


$$\left( \frac{\partial p^{el}}{\partial \rho} \right)_V = \frac{4\pi n Z e^2 / M}{k_0^2}$$

Electronic part dominates, but ...

$(\partial p^{ion}/\partial \rho)_V$  is direction-dependent.

Phonon dispersion relations in gold.



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## Formalism: phonon-induced anisotropy in vdW forces

at  $k = 0.001 \cdot 2\pi/a$ ,  $c_s(\hat{K}) = 5273.5$  m/s,  $c_s(\hat{X}) = 3921.3$  m/s:

$$\begin{aligned}\epsilon(\omega, \mathbf{k} = k\hat{K}) &= \epsilon^{\text{el}}(\omega) \left( 1 - \frac{(3.4 \times 10^{-3})^2}{\omega^2} \right) \\ \epsilon(\omega, \mathbf{k} = k\hat{X}) &= \epsilon^{\text{el}}(\omega) \left( 1 - \frac{(2.5 \times 10^{-3})^2}{\omega^2} \right).\end{aligned}$$

$A_H$  between a rod and gold is (unit:  $k_B T$ )

$$\frac{3}{8\pi} \int d\theta dx x^2 e^{-x} \left( \frac{\epsilon^{rod} - 1 - 2\Delta}{4} \cos^2 \theta + \Delta \right) \left( \frac{\epsilon_z^{gold} - 1}{\epsilon_z^{gold} + 1} \right).$$

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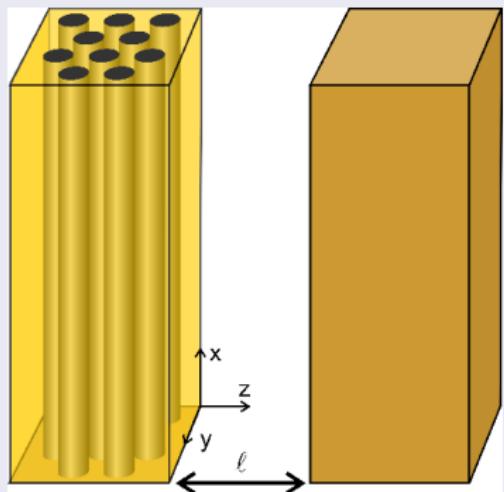
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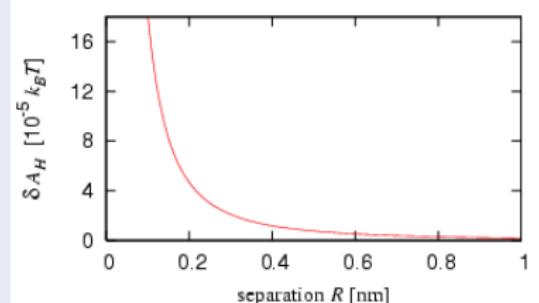
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# Brownian motion and all that

A semi-infinite composite slab on a gold (111) surface



Anisotropy in  $A_H$



$$V(R) = -\frac{A_H a_m^2 \ell_m}{6 R^3},$$

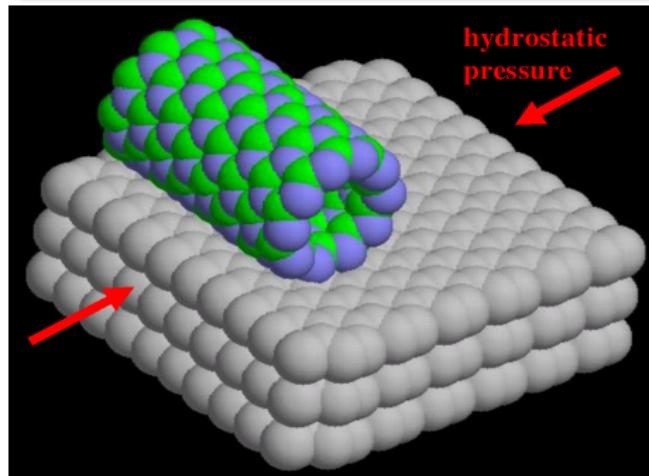
$$\delta V(R = 0.2 \text{ nm}) \approx 2k_B T.$$

# Manipulate a CNT on a polycrystalline substrate

Incorporate phonon screening in the theory of vdW forces

1. Provide a generic mechanism.
2.  $c_s(\hat{k})$  dictates the orientation.

applying an external constraint



# Summary

- Spatial dispersions of  $\epsilon(\omega, \vec{k})$  in the theory of vdW forces.
- Lattice vibrations can induce **anisotropy** in vdW forces.
- A long rod-like object should align along the **slowest sound speed** direction on a metal surface.
- Outlook
  - microscopic theory of vdW forces
  - apply vdW forces beyond pairwise summation in molecular simulations

# Acknowledgment

## Collaborators

- H. C. Schniepp (Chemical Engineering, Princeton)
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- D. A. Saville (Chemical Engineering, Princeton)
- I. A. Aksay (Chemical Engineering, Princeton)
- N. S. Wingreen (Molecular Biology, Princeton)
- R. Car (Chemistry, Princeton)

# References

van der Waals Forces; Molecular Self-Assemblies

Phys. Rev. B **71**, 235412 (2005)

Phys. Rev. Lett. **96**, 18301 (2006)

J. Phys. Chem. B **110**, 16624 (2006)

phonon-induced anisotropic vdW forces, submitted.